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**UNIVERSITI
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College of Engineering
Department of Electronics and Communication Engineering

Test 1 – MODEL ANSWERS

SEMESTER 2, ACADEMIC YEAR 2012/2013

Subject Code : **EEEEB273**
Course Title : **Electronics Analysis & Design II**
Date : **2 November 2012**
Time Allowed : **1½ hours**

Instructions to the candidates:

1. Write your Name and Student ID number. Circle your section number.
2. Write all your answers using pen. **DO NOT USE PENCIL** except for the diagram.
3. **ANSWER ALL QUESTIONS.**
4. **WRITE YOUR ANSWER ON THIS QUESTION PAPER.**

NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.



GOOD LUCK!



Question 1 [30 marks]

For all **BJT current sources** given in **Table 1**, all transistors are matched and have same parameters. The transistor parameters are: $\beta = 50$, $V_{BE(on)} = 0.6 \text{ V}$, and $V_A = 150 \text{ V}$. The circuit parameters for the current sources are: $V^+ = 10 \text{ V}$, $V^- = -10 \text{ V}$, and $R_1 = 24 \text{ k}\Omega$.

- (a) Calculate reference current (I_{REF}), output current (I_O), and output resistance (R_O) for every BJT current source given in the **Table 1** and fill in the **Table 1** with your answers. **Show all calculations** in the area provided after the **Table 1** and **do not forget** to put proper **Units** for I_{REF} , I_O , and R_O in the **Table 1**. [9 marks]

Table 1

BJT current source	Reference current, I_{REF}	Output current, I_O	Output resistance, R_O
1) Three-transistor current source	0.783 mA	0.783 mA	191.57 kΩ
2) Wilson current source	0.783 mA	0.783 mA	4.789 MΩ
3) Cascode current source	0.783 mA	0.725 mA	10.3445 MΩ

[1 mark each box, Total 9 marks]

- (b) Based on the value of R_O , **which current source** has the most stable I_O ? [3 marks]

Cascode [3]

- (c) **Show all your calculations** for I_{REF} , I_O , and R_O for every BJT current source given in the **Table 1** in the following space: [18 marks]

Three-transistor current source	Wilson current source	Cascode current source
$I_{REF} = (V^+ - 2V_{BE} - V^-) / R_1 = (10 - 2 \times 0.6 - (-10)) / (24k) = 0.783 \text{ mA}$ -- same for all CS		
$I_O = I_{REF} / (1 + 2/(\beta(1+\beta)))$ $= (0.783m) / (1 + 2/(50 \times 51))$ $= 0.783 \text{ mA}$	$I_O = I_{REF} / (1 + 2/(\beta(2+\beta)))$ $= (0.783m) / (1 + 2/(50 \times 52))$ $= 0.783 \text{ mA}$	$I_O = I_{REF} / (1 + 4/\beta)$ $= (0.783m) / (1 + 4/(50))$ $= 0.725 \text{ mA}$
$r_{O2} = V_A / I_O$ $= 150 / (0.783m)$ $= 191.57 \text{ k}\Omega$	$r_{O3} = V_A / I_O$ $= 150 / (0.783m)$ $= 191.57 \text{ k}\Omega$	$r_{O4} = V_A / I_O$ $= 150 / (0.725m)$ $= 206.89 \text{ k}\Omega$
$R_O = r_{O2}$ $= 191.57 \text{ k}\Omega$	$R_O = (\beta r_{O3}) / 2$ $= (50 \times 191.57k) / 2$ $= 4.789 \text{ M}\Omega$	$R_O = \beta r_{O4}$ $= 50 \times 206.89k$ $= 10.3445 \text{ M}\Omega$

[2 mark each box, Total 18 marks]

Answer for Question 1

Question 2 [30 marks]

For a MOSFET current source circuit shown in **Figure 2**, the transistor parameters are $V_{TN} = 0.7 \text{ V}$, $k'_n = 60 \mu\text{A/V}^2$, and $\lambda = 0.015 \text{ V}^{-1}$. The transistor aspect ratios are $(W/L)_1 = 20$, $(W/L)_2 = 12$, and $(W/L)_3 = 3$.

- (a) Determine V_{GS1} , I_{REF} , I_O , and V_{DS2} [20 marks]
- (b) Find V_{GS3} [5 marks]
- (c) Find I_O at $V_{DS2} = 3.0 \text{ V}$ [5 marks]

Answer for Question 2

(a)

$$I_{REF} = \frac{k'_n}{2} \left(\frac{W}{L} \right)_1 (V_{GS1} - V_{TN})^2$$

$$I_{REF} = \frac{60\mu}{2} (20) (V_{GS1} - 0.7)^2 \quad [2]$$

$$I_{REF} = \frac{k'_n}{2} \left(\frac{W}{L} \right)_3 (V_{GS3} - V_{TN})^2$$

$$I_{REF} = \frac{60\mu}{2} (3) (V_{GS3} - 0.7)^2 \quad [2]$$

$$V_{GS1} + V_{GS3} = V^+ - V^- = 10$$

$$V_{GS3} = 10 - V_{GS1} \quad [2]$$

$$20(V_{GS1} - 0.7)^2 = 3(10 - V_{GS1} - 0.7)^2$$

$$V_{GS1} = 3.1 \text{ V} \quad [2]$$

$$I_{REF} = \frac{60\mu}{2} (20) (3.1 - 0.7)^2 = 3.456 \text{ mA} \quad [2]$$

$$V_{GS2} = V_{GS1} = 3.1 \text{ V} \quad [3]$$

$$I_O = \frac{k'_n}{2} \left(\frac{W}{L} \right)_2 (V_{GS2} - V_{TN})^2 \quad [2]$$

$$I_O = \frac{60\mu}{2} (12) (3.1 - 0.7)^2 = 2.073 \text{ mA} \quad [3]$$

$$V_{DS2} = V_{DS1} = V_{GS1} = 3.1 \text{ V} \quad [2]$$

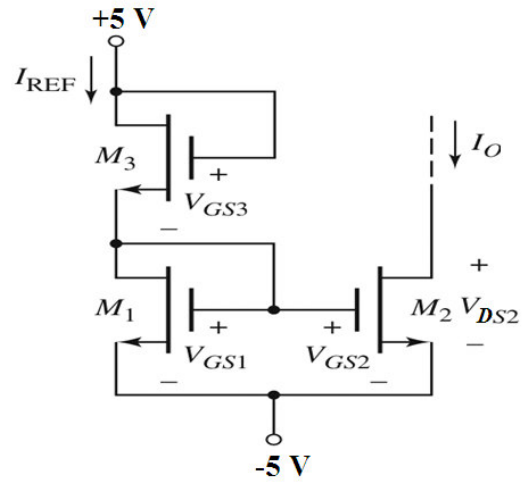


Figure 2

Answer for Question 2

(b) $V_{GS3} = 10 - V_{GS1} = 6.9 \text{ V}$ [5]

(c) $I_O = 2.073 \text{ mA}$ at $V_{DS2} = 3.1 \text{ V}$ [1]

$$R_O = 1/(\lambda I_O) = 1/(0.015 \times 2.073\text{m}) = 32.159 \text{ k}\Omega \quad [1]$$

At $V_{DS2} = 3.0 \text{ V}$,

$$\Delta I_O = (3.0 - 3.1)/R_O = -0.003 \text{ mA} \quad [2]$$

$$\rightarrow I_O = 2.073\text{m} + (-0.003\text{m}) = 2.070 \text{ mA} \quad [1]$$

Question 3 [40 marks]

- (a) **Figure 3a** shows a circuit diagram for a BJT differential amplifier (**diff-amp**). Study the circuit diagram carefully. Transistor parameters are: $\beta = \infty$ (neglect base current), $V_A = \infty$, and $V_{BE(\text{on})} = 0.7 \text{ V}$. For the circuit also, voltages measured at v_{C1} and v_{C2} are **4.5 V**.
- (i) What are the values for v_{cm} and v_d ? Show clearly your calculations. [5 marks]
- (ii) Find I_Q [10 marks]
- (iii) Find v_{CE2} [5 marks]

Answer for Question 3a

(a)

(i)

From Figure 3a:
 $v_{B1} = v_{B2} = 0 \text{ V}$ [1]

→ $v_{cm} = (v_{B1} + v_{B2}) / 2 = 0 \text{ V}$ [2]

→ $v_d = v_{B1} - v_{B2} = 0 \text{ V}$ [2]

(ii)

Given: $v_{C1} = v_{C2} = 4.5 \text{ V}$

$10 - I_{C1}R_C = v_{C1} = 4.5 \text{ V}$ [4]

→ $I_{C1} = 0.55 \text{ mA} = I_{C2}$ [3]

→ $I_Q = I_{C1} + I_{C2} = 1.1 \text{ mA}$ [3]

(iii)

Given: $v_{C2} = 4.5 \text{ V}$

$v_{CE2} = v_{C2} - v_E$ [2]

$v_E = v_{B2} - V_{BE(\text{on})} = 0 - 0.7 = -0.7 \text{ V}$ [2]

→ $v_{CE2} = v_{C2} - v_E = 4.5 - (-0.7) = 5.2 \text{ V}$ [1]

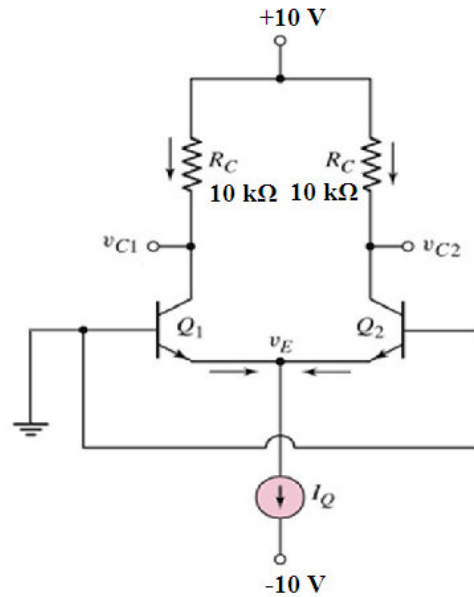


Figure 3a

- (b) The differential amplifier in **Figure 3b** is modified to have a two-transistor current source using **pnp transistors** as an **active load** to replace the passive load resistors R_C . A three-transistor current source using **npn transistors** is also incorporated in the circuit to establish the bias current, I_Q . **Draw the complete NEW circuit** after the circuit in the **Figure 3b** is modified to have the active load and also incorporating the bias circuit mentioned above.

[20 marks]

Answer for Question 3b

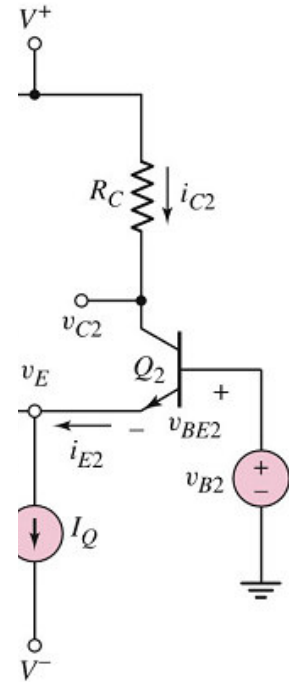
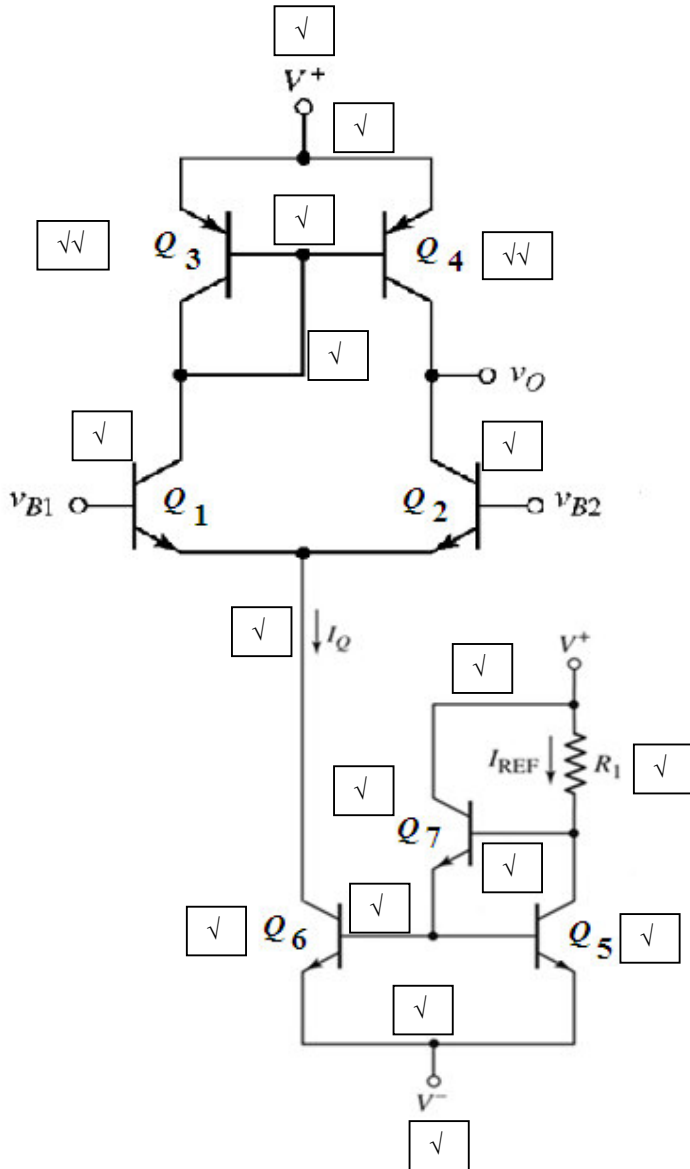


Figure 3b

APPENDIX

BASIC FORMULA

BJT

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

MOSFET

; N – MOSFET

$$v_{DS}(\text{sat}) = v_{GS} - V_{TN}$$

$$i_D = K_n [v_{GS} - V_{TN}]^2$$

$$K_n = \frac{k'_n \cdot W}{2 \cdot L}$$

; P – MOSFET

$$v_{SD}(\text{sat}) = v_{SG} + V_{TP}$$

$$i_D = K_p [v_{SG} + V_{TP}]^2$$

$$K_p = \frac{k'_p \cdot W}{2 \cdot L}$$

; Small signal

$$g_m = 2\sqrt{K_n I_{DQ}}$$

$$r_o \cong \frac{1}{\lambda I_{DQ}}$$