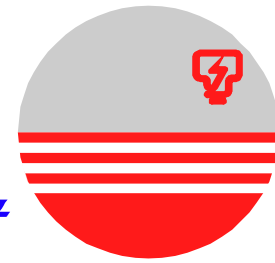


Name:
Student ID Number:
Section: 01/02/03/04 A/B
Lecturer: Dr Jamaludin /Dr Azni Wati
/Dr Fazrena

**UNIVERSITI
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College of Engineering
Department of Electronics and Communication Engineering

Test 1 – Model Answer

SEMESTER 1, ACADEMIC YEAR 2013/2014

Subject Code : **EEEB273**
Course Title : **Electronics Analysis & Design II**
Date : **27 June 2013**
Time Allowed : **1 hour**

Instructions to the candidates:

1. Write your Name and Student ID number. Circle your section number.
2. Write all your answers using pen. **DO NOT USE PENCIL** except for the diagram.
3. **ANSWER ALL QUESTIONS.**
4. **WRITE YOUR ANSWER ON THIS QUESTION PAPER.** Use both sides of the question paper to write your answers.
5. For all calculations, assume that $V_T = 26 \text{ mV}$.

NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.



GOOD LUCK!



FORMULA FOR TRANSISTORS

BJT

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

;Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

MOSFET

;N – MOSFET

$$v_{DS}(\text{sat}) = v_{GS} - V_{TN}$$

$$i_D = K_n [v_{GS} - V_{TN}]^2$$

$$K_n = \frac{k'_n}{2} \cdot \frac{W}{L}$$

;P – MOSFET

$$v_{SD}(\text{sat}) = v_{SG} + V_{TP}$$

$$i_D = K_p [v_{SG} + V_{TP}]^2$$

$$K_p = \frac{k'_p}{2} \cdot \frac{W}{L}$$

;Small signal

$$g_m = 2\sqrt{K_n I_{DQ}}$$

$$r_o \cong \frac{1}{\lambda I_{DQ}}$$

Question 1 [60 marks]

(a) Consider a **modified three-transistor BJT current source** as in **Figure 1(a)**. Transistor parameters are $V_{BE(\text{on})} = 0.7 \text{ V}$, $V_A = \infty$, and $\beta = 80$. *Hint: Please take note of the current directions given in the Figure 1(a).*

(i) **Show that**

$$I_{REF} - \frac{V_{BE}}{(1 + \beta)R_2} = I_O \left(1 + \frac{2}{\beta(1 + \beta)} \right) \quad [20 \text{ marks}]$$

(ii) For $R_2 = 10 \text{ k}\Omega$, $V^+ = 10 \text{ V}$, and $I_O = 0.70 \text{ mA}$, find I_{REF} and R_1 . [20 marks]

Answers for Question 1(a)

(i)

$$I_{B1} = I_{B2} \quad [2]$$

$$I_O = \beta I_{B2} \Rightarrow I_{B2} = I_O / \beta \quad [2]$$

$$I_{C1} = \beta I_{B2} \Rightarrow I_{C1} = I_O \quad [2]$$

$$I_{E3} = 2 I_{B2} + V_{BE} / R_2 \quad [2]$$

$$I_{B3} = I_{E3} / (1 + \beta) \quad [2]$$

$$= (2 I_{B2}) / (1 + \beta) + (V_{BE}) / ((1 + \beta)R_2)$$

$$= (2 I_O) / (\beta(1 + \beta)) + (V_{BE}) / ((1 + \beta)R_2) \quad [2]$$

$$I_{REF} = I_{C1} + I_{B3} \quad [2]$$

$$= I_O + (2 I_O) / (\beta(1 + \beta)) + (V_{BE}) / ((1 + \beta)R_2) \quad [2]$$

$$I_{REF} - (V_{BE}) / ((1 + \beta)R_2) = I_O + (2 I_O) / (\beta(1 + \beta)) \quad [2]$$

$$= I_O [1 + 2 / (\beta(1 + \beta))] \quad [2]$$

$$I_{REF} - \frac{V_{BE}}{(1 + \beta)R_2} = I_O \left(1 + \frac{2}{\beta(1 + \beta)} \right) \quad [2]$$

(ii)

$$I_{REF} = I_O (1 + 2 / (\beta(1 + \beta))) + (V_{BE}) / ((1 + \beta)R_2) \quad [4]$$

$$= (0.70\text{m})(1 + 2 / (80 \times 81)) + (0.7) / (81 \times 10\text{k}) \quad [4]$$

$$= 0.700216\text{m} + 0.000864\text{m}$$

$$= 0.7011 \text{ mA} \quad [2]$$

$$R_1 = (V^+ - 2V_{BE(\text{on})} - 0) / I_{REF} \quad [4]$$

$$= (10 - 2(0.7)) / (0.7011\text{m}) \quad [4]$$

$$= 12.27 \text{ k}\Omega \quad [2]$$

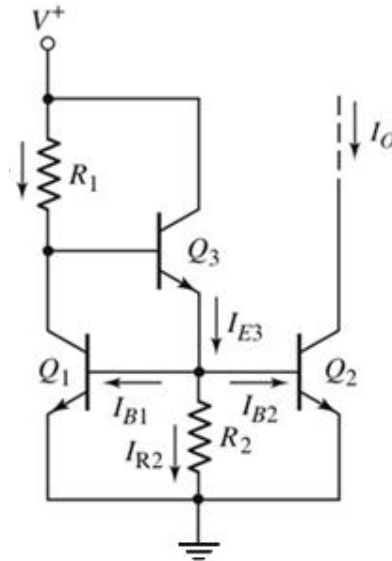


Figure 1(a)

(b) For a MOSFET current source circuit in **Figure 1(b)** the transistor parameters are $V_{TN} = 0.5 \text{ V}$, $k'_n = 80 \mu\text{A}/\text{V}^2$, and $\lambda = 0$. **Design** the circuit such that $V_{DS2}(\text{sat}) = 0.3 \text{ V}$, $I_{REF} = 50 \mu\text{A}$, and the load current is $I_O = 100 \mu\text{A}$.

[20 marks]

Answers for Question 1(b)

$$V_{DS2}(\text{sat}) = V_{GS} - V_{TN} \quad [2]$$

$$\begin{aligned} V_{GS} &= V_{DS2}(\text{sat}) + V_{TN} \\ &= 0.3 + 0.5 = 0.8 \text{ V} \end{aligned} \quad [2]$$

$$I_{REF} = (V^+ - V_{GS} - 0) / R_1 \quad [2]$$

$$\begin{aligned} R_1 &= (V^+ - V_{GS} - 0) / I_{REF} \\ &= (2 - 0.8) / (50\mu) = 24 \text{ k}\Omega \end{aligned} \quad [2]$$

$$I_{REF} = (k'_n / 2) (W/L)_1 [V_{GS} - V_{TN}]^2 \quad [2]$$

$$\begin{aligned} (W/L)_1 &= I_{REF} / \{(k'_n / 2) [V_{GS} - V_{TN}]^2\} \\ &= (50\mu) / \{(80\mu/2) [0.8 - 0.5]^2\} \\ &= 13.889 \end{aligned} \quad [2]$$

$$I_O = (k'_n / 2) (W/L)_2 [V_{GS} - V_{TN}]^2 \quad [2]$$

$$\begin{aligned} (W/L)_2 &= I_O / \{(k'_n / 2) [V_{GS} - V_{TN}]^2\} \\ &= (100\mu) / \{(80\mu/2) [0.8 - 0.5]^2\} \\ &= 27.778 \end{aligned} \quad [2]$$

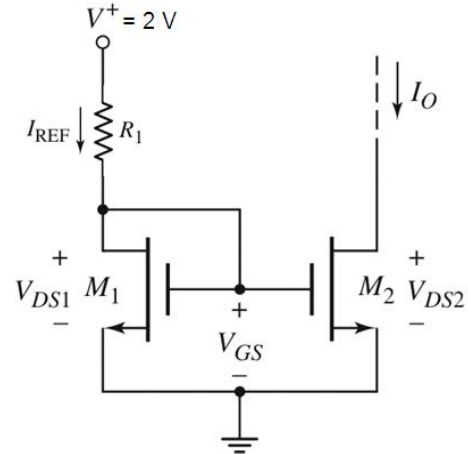


Figure 1(b)

Question 2 [40 marks]

The basic BJT differential pair is shown in **Figure 2**. The circuit parameter values are: $V^+ = +10\text{ V}$, $V^- = -10\text{ V}$, $I_Q = 1\text{ mA}$, and $R_C = 10\text{ k}\Omega$. The transistor parameters in the differential pair are $\beta = \infty$ (neglect base currents), $V_A = \infty$, and $V_{BE(\text{on})} = 0.7\text{ V}$. The constant current source in **Figure 2** that is providing the current I_Q is implemented using the **cascode current source**.

- (i) **Sketch the whole differential pair circuit** to include the circuit for the constant current source circuit. [15 marks]
- (ii) For all transistors in cascode current source, $V_A = 120\text{ V}$ and $\beta = 100$. **What is the value of the output resistance (R_O)** looking into the constant current source? [5 marks]
- (iii) **Determine i_{C1} and v_{CE1}** for common-mode voltages $v_{B1} = v_{B2} = v_{CM} = -5\text{ V}$. [10 marks]
- (iv) It is given that the input voltages for the differential amplifier are $v_{B1} = 210 \times 10^{-6} \sin \omega t\text{ V}$ and $v_{B2} = 190 \times 10^{-6} \sin \omega t\text{ V}$. **Calculate differential-mode input voltage (v_d)** and common-mode input voltage (v_{cm}) of the differential amplifier. [10 marks]

Answers for Question 2

(ii)

$\beta = 100, I_Q = 1\text{ mA}$

For cascode current source

$R_O = (\beta r_{o6})$ [2]

$r_{o6} = V_A / I_Q$ [1]

$= (120)/(1\text{m}) = 120\text{ k}\Omega$ [1]

$R_O = (\beta r_{o6}) = 100 \times 120\text{ k}$ [1]
 $= 12\text{ M}\Omega$

(iii)

$\beta = \infty$

$i_{C1} = i_{E1} = I_Q / 2 = 0.5\text{ mA}$ [3]

$v_{C1} = V^+ - i_{C1} R_C$ [1]

$= 10 - (0.5\text{m})(10\text{k}) = 5\text{ V}$ [1]

For $v_{CM} = -5\text{ V}$

$v_E = v_{CM} - V_{BE(\text{on})}$ [1]

$= -5 - 0.7 = -5.7\text{ V}$ [1]

$v_{CE1} = v_{C1} - v_E$ [2]

$= 5 - (-5.7) = 10.7\text{ V}$ [1]

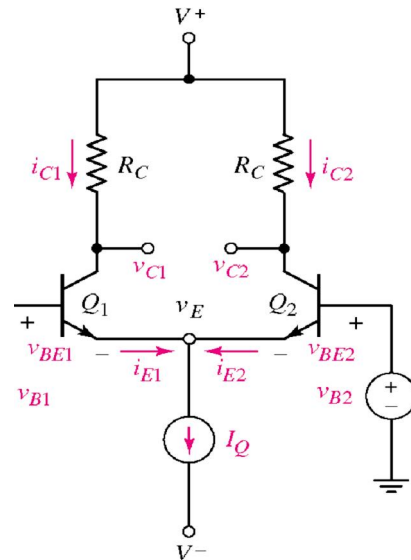


Figure 2

Answers:

(iv)

$$\begin{aligned}v_d &= v_{B1} - v_{B2} && [2] \\ &= 210 \times 10^{-6} \sin \omega t - 190 \times 10^{-6} \sin \omega t && [2] \\ &= 20 \times 10^{-6} \sin \omega t && [1]\end{aligned}$$

$$\begin{aligned}v_{cm} &= (v_{B1} + v_{B2}) / 2 && [2] \\ &= (210 \times 10^{-6} \sin \omega t + 190 \times 10^{-6} \sin \omega t) / 2 && [2] \\ &= 200 \times 10^{-6} \sin \omega t && [1]\end{aligned}$$