

EEEB273 - Quiz 2  
 SEMESTER 2, ACADEMIC YEAR 2013/2014  
 Date: 26 November 2013 Time: 15 minutes

**Question:**

Study **Figure 1** carefully. Assume  $Q_1$  and  $Q_2$  are matched and neglect  $i_B$ . If  $v_d = v_{BE1} - v_{BE2}$ , then show that:

$$i_{C1} = \frac{I_Q}{1 + e^{-v_d/V_T}} \quad [8 \text{ marks}]$$

Given  $V_T = 26 \text{ mV}$ ,  $I_Q = 0.8 \text{ mA}$ , and  $v_d = -0.05 \text{ V}$ ; calculate current  $i_{C1}$ .

[2 marks]

$$i_{C1} = I_S e^{v_{BE1}/V_T} [1]$$

$$i_{C2} = I_S e^{v_{BE2}/V_T} [1]$$

$$I_Q = i_{C1} + i_{C2} [1]$$

$$I_Q = I_S \left[ e^{v_{BE1}/V_T} + e^{v_{BE2}/V_T} \right] [1]$$

$$\frac{i_{C1}}{I_Q} = \frac{1}{1 + e^{(v_{BE2} - v_{BE1})/V_T}} [2]$$

$$v_d = v_{BE1} - v_{BE2} [1]$$

$$i_{C1} = \frac{I_Q}{1 + e^{-v_d/V_T}} [1]$$

$$i_{C1} = \frac{0.8 \text{ mA}}{1 + e^{-(-0.05)/0.026}} = 0.102 \text{ mA} [2]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

EEEE273 - Quiz 2  
SEMESTER 2, ACADEMIC YEAR 2013/2014  
Date: 26 November 2013 Time: 15 minutes

**Question:**

Study **Figure 1** carefully. Assume  $Q_1$  and  $Q_2$  are matched and neglect  $i_B$ . If  $v_d = v_{BE1} - v_{BE2}$ , then show that:

$$i_{C2} = \frac{I_Q}{1 + e^{+v_d/V_T}} \quad [8 \text{ marks}]$$

Given  $V_T = 26 \text{ mV}$ ,  $I_Q = 0.8 \text{ mA}$ , and  $v_d = -0.05 \text{ V}$ ; calculate current  $i_{C2}$ .

[2 marks]

$$i_{C1} = I_S e^{v_{BE1}/V_T} [1]$$

$$i_{C2} = I_S e^{v_{BE2}/V_T} [1]$$

$$I_Q = i_{C1} + i_{C2} [1]$$

$$I_Q = I_S [e^{v_{BE1}/V_T} + e^{v_{BE2}/V_T}] [1]$$

$$\frac{i_{C2}}{I_Q} = \frac{1}{1 + e^{-(v_{BE2} - v_{BE1})/V_T}} [2]$$

$$v_d = v_{BE1} - v_{BE2} [1]$$

$$i_{C2} = \frac{I_Q}{1 + e^{+v_d/V_T}} [1]$$

$$i_{C2} = \frac{0.8 \text{ mA}}{1 + e^{(-0.05)/0.026}} = 0.698 \text{ mA} [2]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{ npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{ pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

EEEB273 - Quiz 2  
SEMESTER 2, ACADEMIC YEAR 2013/2014  
Date: 26 November 2013 Time: 15 minutes

**Question:**

Study **Figure 1** carefully. Assume  $Q_1$  and  $Q_2$  are matched and neglect  $i_B$ . If  $v_d = v_{BE1} - v_{BE2}$ , then show that:

$$i_{C1} = \frac{I_Q}{1 + e^{-v_d/V_T}} \quad [8 \text{ marks}]$$

Given  $V_T = 26 \text{ mV}$ ,  $I_Q = 0.7 \text{ mA}$ , and  $v_d = +0.05 \text{ V}$ ; calculate current  $i_{C1}$ .

[2 marks]

$$i_{C1} = I_S e^{v_{BE1}/V_T} [1]$$

$$i_{C2} = I_S e^{v_{BE2}/V_T} [1]$$

$$I_Q = i_{C1} + i_{C2} [1]$$

$$I_Q = I_S [e^{v_{BE1}/V_T} + e^{v_{BE2}/V_T}] [1]$$

$$\frac{i_{C1}}{I_Q} = \frac{1}{1 + e^{(v_{BE2} - v_{BE1})/V_T}} [2]$$

$$v_d = v_{BE1} - v_{BE2} [1]$$

$$i_{C1} = \frac{I_Q}{1 + e^{-v_d/V_T}} [1]$$

$$i_{C1} = \frac{0.7 \text{ mA}}{1 + e^{-(0.05)/0.026}} = 0.6107 \text{ mA} [2]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

EEEB273 - Quiz 2  
 SEMESTER 2, ACADEMIC YEAR 2013/2014  
 Date: 26 November 2013 Time: 15 minutes

**Question:**

Study **Figure 1** carefully. Assume  $Q_1$  and  $Q_2$  are matched and neglect  $i_B$ . If  $v_d = v_{BE1} - v_{BE2}$ , then show that:

$$i_{C2} = \frac{I_Q}{1 + e^{+v_d/V_T}} \quad [8 \text{ marks}]$$

Given  $V_T = 26 \text{ mV}$ ,  $I_Q = 0.7 \text{ mA}$ , and  $v_d = +0.05 \text{ V}$ ; calculate current  $i_{C2}$ . [2 marks]

$$i_{C1} = I_S e^{v_{BE1}/V_T} [1]$$

$$i_{C2} = I_S e^{v_{BE2}/V_T} [1]$$

$$I_Q = i_{C1} + i_{C2} [1]$$

$$I_Q = I_S \left[ e^{v_{BE1}/V_T} + e^{v_{BE2}/V_T} \right] [1]$$

$$\frac{i_{C2}}{I_Q} = \frac{1}{1 + e^{-(v_{BE2} - v_{BE1})/V_T}} [1]$$

$$v_d = v_{BE1} - v_{BE2} [1]$$

$$i_{C2} = \frac{I_Q}{1 + e^{+v_d/V_T}} [1]$$

$$i_{C2} = \frac{0.7 \text{ mA}}{1 + e^{(0.05)/0.026}} = 0.0893 \text{ mA} [2]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{ npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{ pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_o = \frac{V_A}{I_{CQ}}$$