

Question:

A **Widlar current source** circuit to be designed has the configuration shown in **Figure 1**. The circuit parameters are: $V^+ = +5.5 \text{ V}$ and $V^- = -5.5 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 80 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

- (a) Design the Widlar current source circuit such that $I_{REF} = 1 \text{ mA}$ and $I_O = 12 \mu\text{A}$. [4 marks]
 (b) Find V_{BE2} . [2 marks]
 (c) Calculate the output resistance (R_O) of the Widlar current source in **Figure 1** using the following formula. Use parameters and results from **part (a)** above. [4 marks]

$$R_O = r_{o2} [1 + g_{m2} (R_E \parallel r_{\pi 2})]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{ npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{ pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

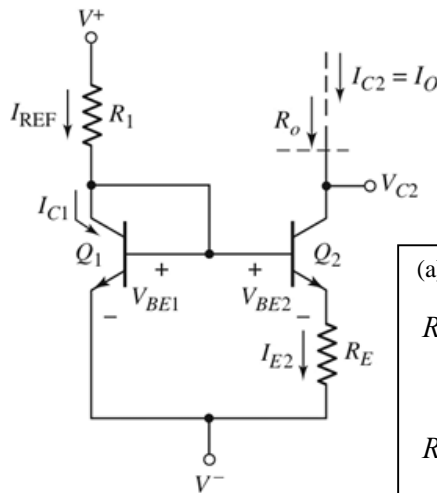


Figure 1

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5.5 - 0.6 - (-5.5)}{1\text{m}} = 10.4\text{k}\Omega$$
 [2]

$$R_E = \frac{V_T}{I_O} \ln\left(\frac{I_{REF}}{I_O}\right) = \frac{0.026}{12} \ln\left(\frac{1\text{m}}{12}\right) = 9.58\text{k}\Omega$$
 [2]

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (12 \mu\text{A})(9.58\text{k}) = 0.485\text{V}$$
 [2]

(c)
$$g_{m2} = \frac{I_O}{V_T} = \frac{12\mu}{0.026} = 0.462\text{mA/V}$$
 [1]

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{12\mu} = 260\text{k}\Omega$$
 [1]

$$r_{o2} = \frac{V_A}{I_O} = \frac{80}{12\mu} = 6.67\text{M}\Omega$$
 [1]

$$R_O = r_{o2} [1 + g_{m2} (R_E \parallel r_{\pi 2})]$$

$$R_O = (6.67\text{M}) [1 + (0.462\text{m})(9.58\text{k} \parallel 260\text{k})] = 35.1\text{M}\Omega$$
 [1]

Question:

A **Widlar current source** circuit to be designed has the configuration shown in **Figure 1**. The circuit parameters are: $V^+ = +5.0 \text{ V}$ and $V^- = -5.0 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 80 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

- (a) Design the Widlar current source circuit such that $I_{REF} = 1.2 \text{ mA}$ and $I_O = 12 \text{ }\mu\text{A}$. [4 marks]
- (b) Find V_{BE2} . [2 marks]
- (c) Calculate the output resistance (R_O) of the Widlar current source in **Figure 1** using the following formula. Use parameters and results from **part (a)** above. [4 marks]

$$R_O = r_{o2} \left[1 + g_{m2} (R_E \parallel r_{\pi 2}) \right]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{ npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{ pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

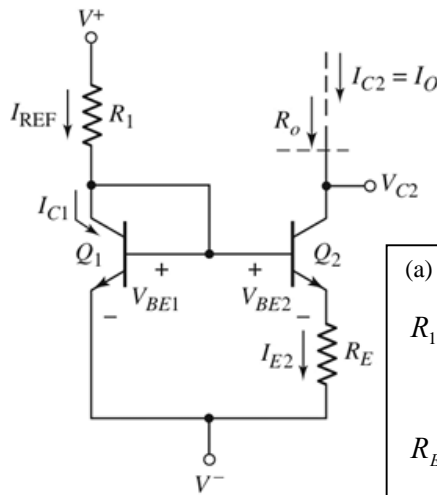


Figure 1

Answer:

(a)

$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5 - 0.6 - (-5)}{1.2\text{m}} = 7.83\text{k}\Omega \quad [2]$$

$$R_E = \frac{V_T}{I_O} \ln \left(\frac{I_{REF}}{I_O} \right) = \frac{0.026}{12} \ln \left(\frac{1.2\text{m}}{12} \right) = 9.98\text{k}\Omega \quad [2]$$

(b)

$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (12 \mu\text{A})(9.98\text{k}) = 0.48\text{V} \quad [2]$$

(c)

$$g_{m2} = \frac{I_O}{V_T} = \frac{12\mu}{0.026} = 0.462\text{mA/V} \quad [1]$$

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{12\mu} = 260\text{k}\Omega \quad [1]$$

$$r_{o2} = \frac{V_A}{I_O} = \frac{80}{12\mu} = 6.67\text{M}\Omega \quad [1]$$

$$R_O = r_{o2} \left[1 + g_{m2} (R_E \parallel r_{\pi 2}) \right]$$

$$R_O = (6.67\text{M}) \left[1 + (0.462\text{m})(9.98\text{k} \parallel 260\text{k}) \right] = 36.2\text{M}\Omega \quad [1]$$

Question:

A **Widlar current source** circuit to be designed has the configuration shown in **Figure 1**. The circuit parameters are: $V^+ = +5.0 \text{ V}$ and $V^- = -5.0 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 100 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

- (a) Design the Widlar current source circuit such that $I_{REF} = 1 \text{ mA}$ and $I_O = 10 \mu\text{A}$. [4 marks]
 (b) Find V_{BE2} . [2 marks]
 (c) Calculate the output resistance (R_O) of the Widlar current source in **Figure 1** using the following formula. Use parameters and results from **part (a)** above. [4 marks]

$$R_O = r_{o2} \left[1 + g_{m2} (R_E \parallel r_{\pi 2}) \right]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{ npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{ pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

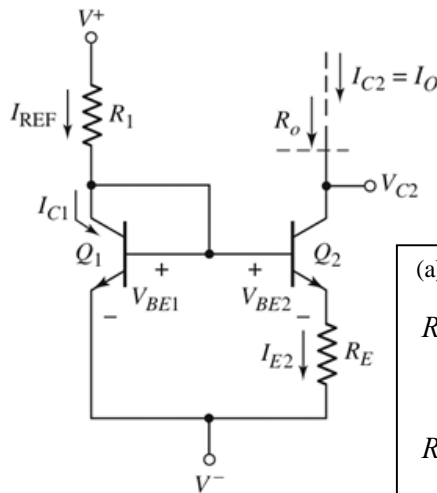


Figure 1

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5 - 0.6 - (-5)}{1\text{m}} = 9.40\text{k}\Omega \quad [2]$$

$$R_E = \frac{V_T}{I_O} \ln\left(\frac{I_{REF}}{I_O}\right) = \frac{0.026}{10} \ln\left(\frac{1\text{m}}{10}\right) = 11.97\text{k}\Omega \quad [2]$$

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (10 \mu\text{A})(11.97\text{k}) = 0.48\text{V} \quad [2]$$

(c)
$$g_{m2} = \frac{I_O}{V_T} = \frac{10\mu}{0.026} = 0.385\text{mA/V} \quad [1]$$

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{10\mu} = 312\text{k}\Omega \quad [1]$$

$$r_{o2} = \frac{V_A}{I_O} = \frac{100}{10\mu} = 10.0\text{M}\Omega \quad [1]$$

$$R_O = r_{o2} \left[1 + g_{m2} (R_E \parallel r_{\pi 2}) \right]$$

$$R_O = (10.0\text{M}) \left[1 + (0.385\text{m})(11.97\text{k} \parallel 312\text{k}) \right] = 54.3\text{M}\Omega \quad [1]$$

Question:

A Widlar current source circuit to be designed has the configuration shown in **Figure 1**. The circuit parameters are: $V^+ = +5.5 \text{ V}$ and $V^- = -5.5 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 100 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

- (a) Design the Widlar current source circuit such that $I_{REF} = 1 \text{ mA}$ and $I_O = 10 \mu\text{A}$. [4 marks]
- (b) Find V_{BE2} . [2 marks]
- (c) Calculate the output resistance (R_O) of the Widlar current source in **Figure 1** using the following formula. Use parameters and results from **part (a)** above. [4 marks]

$$R_O = r_{o2} [1 + g_{m2} (R_E \parallel r_{\pi 2})]$$

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

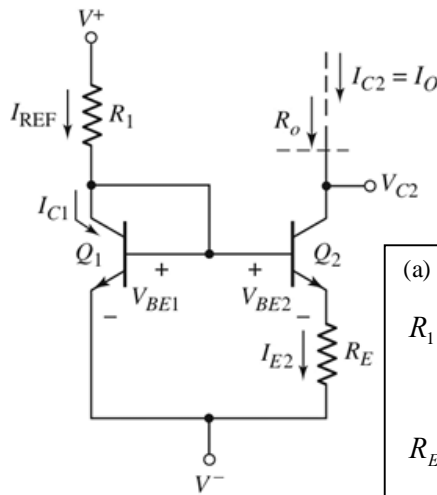


Figure 1

Answer:

(a)

$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5.5 - 0.6 - (-5.5)}{1\text{m}} = 10.4\text{k}\Omega \quad [2]$$

$$R_E = \frac{V_T}{I_O} \ln\left(\frac{I_{REF}}{I_O}\right) = \frac{0.026}{10} \ln\left(\frac{1\text{m}}{10}\right) = 11.97\text{k}\Omega \quad [2]$$

(b)

$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (10 \mu\text{A})(11.97\text{k}) = 0.48\text{V} \quad [2]$$

(c)

$$g_{m2} = \frac{I_O}{V_T} = \frac{10\mu}{0.026} = 0.385\text{mA/V} \quad [1]$$

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{10\mu} = 312\text{k}\Omega \quad [1]$$

$$r_{o2} = \frac{V_A}{I_O} = \frac{100}{10\mu} = 10.0\text{M}\Omega \quad [1]$$

$$R_O = r_{o2} [1 + g_{m2} (R_E \parallel r_{\pi 2})]$$

$$R_O = (10.0\text{M}) [1 + (0.385\text{m})(11.97\text{k} \parallel 312\text{k})] = 54.3\text{M}\Omega \quad [1]$$