



**COLLEGE OF ENGINEERING
PUTRAJAYA CAMPUS
FINAL EXAMINATION**

SEMESTER 2 2015 / 2016

MODEL ANSWER

PROGRAMME : Bachelor of Electrical & Electronics Engineering (Honours)
Bachelor of Electrical Power Engineering (Honours)

SUBJECT CODE : EEEB273

SUBJECT : ELECTRONIC ANALYSIS AND DESIGN II

DATE : February 2016

TIME : 3 hours

INSTRUCTIONS TO CANDIDATES:

1. This paper contains **FIVE** (5) questions in **NINE** (9) pages.
2. Answer **ALL** questions.
3. Write **all** answers in the answer booklet provided. Use **pen** to write your answer.
4. Write answer to different question on a **new page**.
5. Show clearly all calculations, complete with proper Unit for every parameter.

THIS QUESTION PAPER CONSISTS OF NINE (9) PRINTED PAGES INCLUDING THIS COVER PAGE.

Question 1 [20 marks]

Question 1(a) [7.5 marks]

$$R_1 = \frac{V^+ - V_{BE5} - V_{BE3} - V^-}{I_{REF}} = \frac{10 - 0.7 - 0.7 - (-10)}{0.5mA} = 37.2k\Omega \quad [1, 1, 0.5]$$

$$I_Q = \frac{I_{REF}}{1 + 4/\beta} = \frac{0.5m}{1 + 4/50} = 0.4629mA \quad [1, 1, 0.5]$$

$$R_O = \beta_6 r_{o6} = \beta_6 \frac{V_{A6}}{I_Q} = 50 \frac{250}{0.4629m} = 27.003M\Omega \quad [1, 1, 0.5]$$

Question 1(b) [5 marks]

$$A_d = \frac{g_{m2} R_C}{2}$$

$$R_C = \frac{2A_d}{g_{m2}} = \frac{2(200)}{8.903m} = 44.928k\Omega \quad [1, 1, 0.5]$$

$$g_{m2} = \frac{I_Q/2}{V_T} = \frac{0.4629m}{2(0.026)} = 8.903mA/V \quad [1, 1, 0.5]$$

Question 1(c) [6 marks]

$$A_{cm} = \frac{-g_{m2} R_C}{1 + \frac{2(1 + \beta_2) R_O}{r_{\pi 2}}}$$

$$R_O = 27.003M\Omega$$

$$g_{m2} = 8.903mA/V$$

$$R_C = 44.928k\Omega$$

$$r_{\pi 2} = \frac{\beta_2 V_T}{I_Q/2} = \frac{2(150)(0.026)}{0.4629m} = 16.85k\Omega \quad [1, 1, 0.5]$$

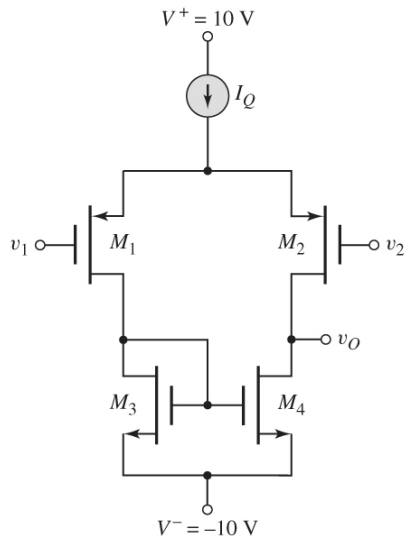
$$A_{cm} = \frac{-g_{m2} R_C}{1 + \frac{2(1 + \beta_2) R_O}{r_{\pi 2}}} = \frac{-(8.903m)(44.928k)}{1 + \frac{2(1 + 150)(27.003M)}{16.85k}} = -0.000826V/V \quad [1, 2, 0.5]$$

Question 1(d) [1.5 marks]

Increase R_O of the cascode current source.

Question 2 [20 marks]

Q2(a)



\$M_3\$ and \$M_4\$ labels [2]

Placement of NMOS CS [2]

\$V_O\$ placement [1]

Q2(b)

Based on symmetry, $V_{GS3} = V_{GS4}$; $V_{DS3} = V_{DS4}$

$$V_{GS} = V_{TN} + \sqrt{\frac{I_{REF}}{K_n}}; \quad [2]$$

$$\text{thus } V_{GS3} = V_{GS4} = V_{DS3} = V_{DS4} = 1 + \sqrt{\frac{0.2\text{mA}/2}{0.1\text{mA}}} = \underline{2\text{ V}} \quad [1]$$

$$V_{SG1} = V_{SG2} = 1 + \sqrt{\frac{0.2\text{mA}/2}{0.1\text{mA}}} = \underline{2\text{ V}} \quad [1]$$

$$V_{SD1} = V_{SD2} = V_{GS1} \text{ ó } (V_{DS3} \text{ ó } 10) = 2 \text{ ó } (2 \text{ ó } 10) = \underline{10\text{ V}} \quad [1]$$

Q2(c)

$$r_{On} = \frac{1}{\lambda_n I_{DQ}} \quad [1] = \frac{1}{(0.01)(0.1\text{mA})} = \underline{1\text{ M}\Omega} \quad [1]$$

$$r_{Op} = \frac{1}{\lambda_p I_{DQ}} = \frac{1}{(0.015)(0.1\text{mA})} = \underline{0.667\text{ M}\Omega} \quad [1]$$

$$A_d = g_m(r_{on} \parallel r_{op}) \quad [1] = (0.2)(1000\text{k} \parallel 667\text{k}) = \underline{80} \quad [1]$$

Q2(d)

$$I_{D1} = I_{D2} = I_Q/2 = \underline{0.1\text{ mA}} \quad [1]$$

$$\text{As } r_{o2} = r_{on} = \underline{1\text{ M}\Omega} \quad [0.5] \text{ and } r_{o4} = r_{op} = \underline{0.667\text{ M}\Omega} \quad [0.5]$$

$$\text{Therefore, RO} = r_{o2} \parallel r_{o4} \quad [2] = (1000\text{k} \parallel 667\text{k}) = \underline{400\text{ k}\Omega} \quad [1]$$

Question 3 [20 marks]

Answer:

Q3(a)

$$i_{E1min} = I_Q - |i_{Lmin}| \quad [1]$$

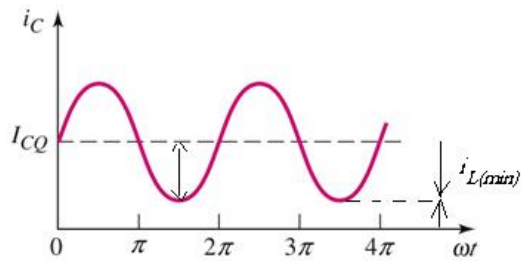
$$P_L = \frac{V_p^2}{2R_L} = 50mW \quad [2]$$

$$V_p = \sqrt{2R_L P_L} = 1.581V \quad [1]$$

$$|i_{Lmin}| = \frac{V_p}{R_L} = \frac{1.581}{25} = 63.24mA \quad [1]$$

$$I_Q - i_{E1} = 0.8I_Q = |i_{Lmin}| \quad [1]$$

$$I_Q = \frac{63.24mA}{0.8} = 79.05mA \quad [1]$$



$$R = \frac{0 - V_{BE(on)} - V^-}{I_Q} = \frac{-0.7 + 12}{79.05mA} = 143\Omega \quad [3]$$

Q3(b)

$$I_{C1} = \frac{\beta}{1+\beta} I_{B2} = \frac{I_{C2}}{1+\beta} = \frac{1mA}{61} = 16.39\mu A \quad [2]$$

$$r_{\pi1} = \frac{(60)(0.026)}{16.39\mu} = 95.18k\Omega \quad [1]$$

$$r_{\pi2} = \frac{(60)(0.026)}{1mA} = 1.56k\Omega \quad [1]$$

$$R_i = r_{\pi1} + (1 + \beta)r_{\pi2} = 95.18k + (61)(1.56k) = 190.3k\Omega \quad [2]$$

$$r_{\pi3} = \frac{(60)(0.026)}{5mA} = 312\Omega \quad [1]$$

$$R_o = 5k \parallel \left[\frac{r_{\pi3} + 50k}{1+\beta} \right] = 5k \parallel 825 = 708\Omega \quad [3]$$

Question 4 [20 marks]

Answer:

$$A_{d1} = g_{m2}(r_{o2} \parallel r_{o4}) = 243 \quad [1] \text{ or Total [5]}$$

$$A_{v2} = g_{m7}(r_{o7} \parallel r_{o8}) = 272 \quad [1] \text{ or Total [5]}$$

Overall gain

$$A_d = [g_{m2}(r_{o2} \parallel r_{o4})]X[g_{m7}(r_{o7} \parallel r_{o8})] = 66010 \quad [2]$$

$$I_{D5} = K_p [V_{SG5} + V_{TP}]^2 = \frac{V^1 - V - V_{SG5}}{R_{SEE}} \quad [2]$$

$$60V_{SG5}^2 - 71V_{SG5} + 11.6 = 0 \quad [2]$$

$$V_{SG5} = 0.987V \gg I_{D5} = 60.0\mu A \quad [1, 1]$$

$$I_{D5} = I_Q = I_{D7} \quad [1]$$

$$I_{D7} = \frac{I_Q}{2} = 30.0\mu A \quad [1]$$

Elements in A_{d1} and A_{v2}

K_{n7}	K_{p2}	g_{m2}	g_{m7}
1 mA/V ²	0.4 mA/V ²	0.2191mA/V	0.4899mA/V
[1]	[1]	[1]	[1]

r_{o2}	r_{o4}	r_{o7}	r_{o8}
2.218Má	2.218Má	1.109Má	1.109Má
[1]	[1]	[1]	[1]

Question 5 [20 marks]

Answers:

Q5(a)

Calculation:

$$A_v = 1 + R_2/(R_{1F} + R_{1V}) \quad [1]$$

$$R_2 = 250 \text{ k} \quad . \quad R_{1F} \text{ is a fixed-value resistor.}$$

R_{1V} is a potentiometer. Gain is maximum, i.e. 51, when $R_{1V} = 0$.

$$A_{v1} = 51 = 1 + R_2/(R_{1F} + R_{1V}) = 1 + 250\text{k}/(R_{1F} + 0) \quad [1]$$

$$R_{1F} = 5 \text{ k} \quad [0.5]$$

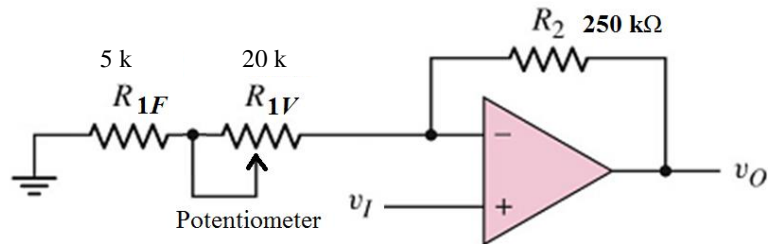
Gain is minimum, i.e. 11, when R_{1V} is maximum.

$$A_{v2} = 11 = 1 + R_2/(R_{1F} + R_{1V}) = 1 + 250\text{k}/(5\text{k} + R_{1V}) \quad [1]$$

$$R_{1V} = 20 \text{ k} \quad [0.5]$$

Circuit:

[2]



Q5(b)

$$\begin{aligned} v_{O1} &= (-R_F/R_1) v_{I1} + (-R_F/R_2) v_{I2} \\ &= (-R_F/R_1) v_{I1} + (-R_F/R_1) v_{I2} \\ &= (-R_F/R_1) (v_{I1} + v_{I2}) \end{aligned} \quad [3]$$

$$v_O = (-R_F/R_1) v_{O1} \quad [1]$$

$$= (-R_F/R_1) (-R_F/R_1) (v_{I1} + v_{I2}) \quad [1]$$

$$= (-100\text{k}/100\text{k}) (-100\text{k}/100\text{k}) (v_{I1} + v_{I2})$$

$$= v_{I1} + v_{I2} \quad [1]$$

Note: Student can use any method that leads to the same answer.

$$v_O = -10v_{I1} - 5v_{I2} + 2v_{I3} + 5v_{I4}$$

Q5(c)

$$R_F / R_1 = 10 \quad \rightarrow \quad R_F = 10 R_1 \quad [0.5]$$

and $R_F / R_2 = 5 \quad \rightarrow \quad R_F = 5 R_2 \quad [0.5]$

So, resistor R_1 will be the **smallest** value. Set $R_1 = 25 \text{ k}\Omega$. [1]

$$\rightarrow R_F = 10 R_1 = 10 \times 25 \text{ k} = 250 \text{ k}\Omega \quad [0.5]$$

and $R_2 = R_F / 5 = 250 \text{ k} / 5 = 50 \text{ k}\Omega \quad [0.5]$

$$R_N = R_1 \parallel R_2 = 25 \text{ k} \parallel 50 \text{ k} = 16.667 \text{ k}\Omega$$

$$1 + R_F / R_N = 1 + 250 \text{ k} / (16.667 \text{ k}) = 16$$

$$(1 + R_F / R_N)(R_P / R_A) = (16)(R_P / R_A) = 2 \quad [0.5]$$

and $(1 + R_F / R_N)(R_P / R_B) = (16)(R_P / R_B) = 5 \quad [0.5]$

So, $(R_A / R_B) = 5/2$. [0.5]

Choose $R_B = 80 \text{ k}\Omega$, [1]

then $R_A = 200 \text{ k}\Omega$ [1]

$$R_P = (5 R_B) / 16 = (2 R_A) / 16$$

$$\rightarrow R_P = 25 \text{ k}\Omega \quad [0.5]$$

$$R_P = R_A \parallel R_B \parallel R_C$$

$$\rightarrow R_C = 44.45 \text{ k}\Omega \quad [1]$$