

**Question:**

Refer to the Wilson current source shown in Figure 1. Assume the reference current  $I_{REF}$  is 0.25 mA. The transistor parameters are  $V_{BE}(\text{on}) = 0.7 \text{ V}$ ,  $V_A = 120 \text{ V}$ , and  $\beta = 80$ .

- (a) Determine the output resistance  $R_O$  looking into the collector of  $Q_3$ . [7 marks]  
 (b) What is the change in  $I_O$  as the output voltage change by +5 Volts? [3 marks]

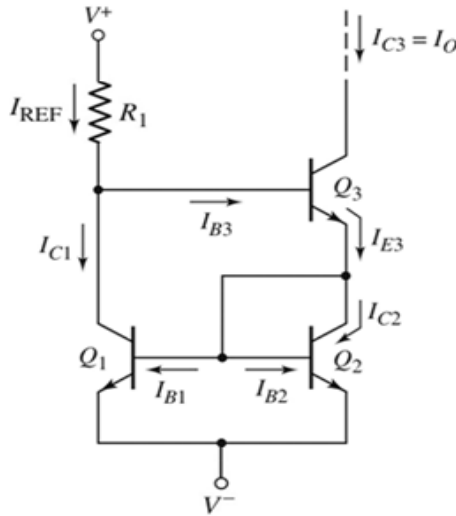


Figure 1

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

**Answer:**

(a)		
$I_O$	$= I_{REF} / [1 + 2/\beta(2+\beta)]$	[1]
	$= (0.25\text{m})/[1 + 2/(80 \times 82)]$	[1]
	$= 0.2499 \text{ mA}$	[1]
$R_O$	$= (\beta r_{o3}) / 2 = (\beta V_A) / (2 I_O)$	[2]
	$= (80 \times 120) / (2 \times 0.2499\text{m})$	[1]
	$= 19.205 \text{ M}\Omega$	[1]
(b)		
$I_O$	$= dV_O / R_O$	[1]
	$= 5 / 19.205\text{M}$	[1]
	$= 0.26 \mu\text{A}$	[1]

**Question:**

Refer to the Wilson current source shown in Figure 1. Assume the reference current  $I_{REF}$  is 0.25 mA. The transistor parameters are  $V_{BE(on)} = 0.7$  V,  $V_A = 100$  V, and  $\beta = 80$ .

- (a) Determine the output resistance  $R_O$  looking into the collector of  $Q_3$ . [7 marks]  
 (b) What is the change in  $I_O$  as the output voltage change by +4.5 Volts? [3 marks]

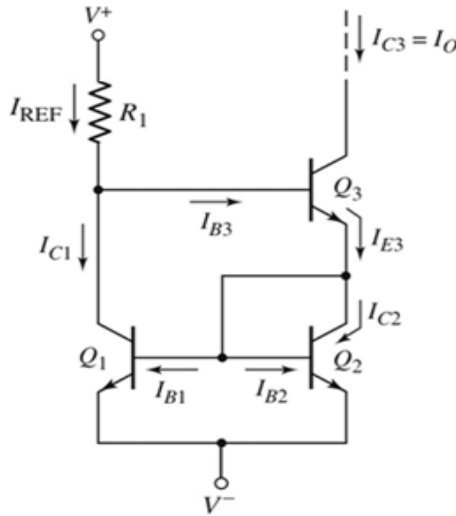


Figure 1

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$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

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; Small signal

$$\beta = g_m r_\pi$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

**Answer:**

(a)		
$I_O$	$= I_{REF} / [1 + 2/\beta(2+\beta)]$	[1]
	$= (0.25\text{m})/[1 + 2/(80 \times 82)]$	[1]
	$= 0.2499 \text{ mA}$	[1]
$R_O$	$= (\beta r_{o3}) / 2 = (\beta V_A) / (2 I_O)$	[2]
	$= (80 \times 100) / (2 \times 0.2499\text{m})$	[1]
	$= 16.004 \text{ M}\Omega$	[1]
(b)		
$I_O$	$= dV_O / R_O$	[1]
	$= 4.5 / 16.004\text{M}$	[1]
	$= 0.281 \mu\text{A}$	[1]

**Question:**

Refer to the Wilson current source shown in Figure 1. Assume the reference current  $I_{REF}$  is 0.25 mA. The transistor parameters are  $V_{BE}(\text{on}) = 0.7 \text{ V}$ ,  $V_A = 120 \text{ V}$ , and  $\beta = 90$ .

- (a) Determine the output resistance  $R_O$  looking into the collector of  $Q_3$ . [7 marks]  
 (b) What is the change in  $I_O$  as the output voltage change by +4.5 Volts? [3 marks]

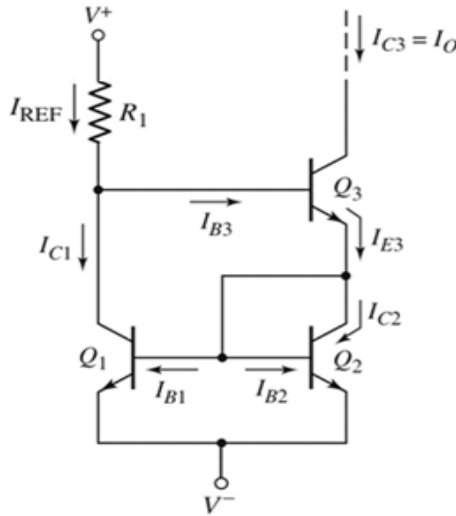


Figure 1

**Answer:**

(a)		
$I_O$	$= I_{REF} / [1 + 2/\beta(2+\beta)]$	[1]
	$= (0.25\text{m})/[1 + 2/(90 \times 92)]$	[1]
	$= 0.2499 \text{ mA}$	[1]
$R_O$	$= (\beta r_{o3}) / 2 = (\beta V_A) / (2 I_O)$	[2]
	$= (90 \times 120) / (2 \times 0.2499\text{m})$	[1]
	$= 21.605 \text{ M}\Omega$	[1]
(b)		
$I_O$	$= dV_O / R_O$	[1]
	$= 4.5 / 21.605\text{M}$	[1]
	$= 0.208 \mu\text{A}$	[1]

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

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$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$$\beta = g_m r_\pi$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

**Question:**

Refer to the Wilson current source shown in Figure 1. Assume the reference current  $I_{REF}$  is 0.25 mA. The transistor parameters are  $V_{BE}(\text{on}) = 0.7 \text{ V}$ ,  $V_A = 100 \text{ V}$ , and  $\beta = 90$ .

- (a) Determine the output resistance  $R_O$  looking into the collector of  $Q_3$ . [7 marks]  
 (b) What is the change in  $I_O$  as the output voltage change by +5 Volts? [3 marks]

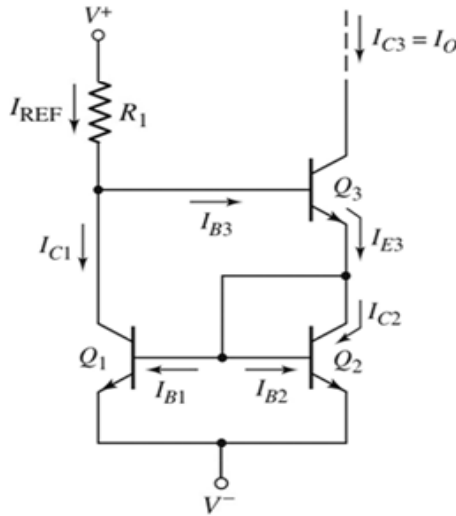


Figure 1

**Answer:**

(a)		
$I_O$	$= I_{REF} / [1 + 2/\beta(2+\beta)]$	[1]
	$= (0.25\text{m})/[1 + 2/(90 \times 92)]$	[1]
	$= 0.2499 \text{ mA}$	[1]
$R_O$	$= (\beta r_{O3}) / 2 = (\beta V_A) / (2 I_O)$	[2]
	$= (90 \times 100) / (2 \times 0.2499\text{m})$	[1]
	$= 18.004 \text{ M}\Omega$	[1]
(b)		
$I_O$	$= dV_O / R_O$	[1]
	$= 5 / 18.004\text{M}$	[1]
	$= 0.278 \mu\text{A}$	[1]

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$$r_o = \frac{V_A}{I_{CQ}}$$