

EEEE273 - Quiz 1
 SEMESTER 2, ACADEMIC YEAR 2016/2017
 Date: 25 October 2016 Time: 15 minutes

Question:

Refer to **Figure 1**. All transistors are matched.

The circuit parameters are: $V^+ = 7.5 \text{ V}$ and $V^- = -7.5 \text{ V}$.

The transistor parameters are: $\beta = 100$, $V_{BE(\text{on})} = 0.6 \text{ V}$, and $V_A = 150 \text{ V}$.

(a) **Design** a two-transistor current source using all the parameters given above so that $I_{B2} = 6 \mu\text{A}$.

[4.5 marks]

(b) Find the **change in I_O** (i.e. dI_O) if $V_{C2} = 3.2 \text{ V}$.

[5.5 marks]

Show clearly all calculations as marks are given according to this.

Answer:

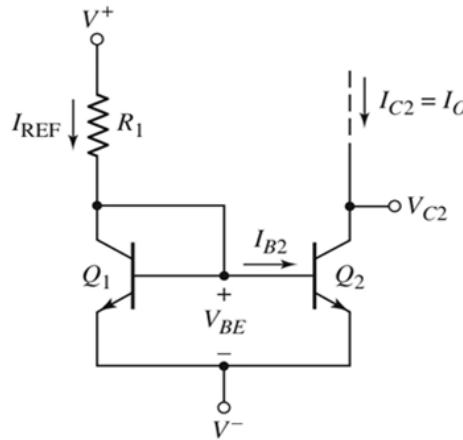


Figure 1

$$i_C = I_S e^{v_{BE}/V_T}; \text{npn}$$

$$i_C = I_S e^{v_{EB}/V_T}; \text{pnp}$$

$$i_C = \alpha i_E = \beta i_B$$

$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$I_O = I_{C2}$	$= \beta I_{B2}$	[1]	$r_o = g_m r_\pi$ $r_m = \frac{I_{CQ}}{V_T}$ $r_e = \frac{\beta V_T}{I_{CQ}}$ $r_o = \frac{V_A}{I_{CQ}}$ $r_T = 26 \text{ mV}$
	$= (100)(6\mu) = 0.6 \text{ mA}$	[0.5]	
I_{REF}	$= I_O (1 + 2/\beta)$	[1]	
	$= (0.6\text{m})(1 + 2/100) = 0.612 \text{ mA}$	[0.5]	
R_1	$= (V^+ - V_{BE} - V^-) / I_{REF}$	[1]	
	$= (7.5 - 0.6 - (-7.5)) / (0.612\text{m}) = 23.529 \text{ k}\Omega$	[0.5]	
R_O	$= r_{o2} = V_A / I_O$	[1]	
	$= (150) / (0.6\text{m}) = 250 \text{ k}\Omega$	[0.5]	
Ori_ V_{CE2}	$= V_{CE1} = V_{BE(\text{on})} = 0.6 \text{ V}$	[1]	
New_ V_{CE2}	$= V_{C2} - V^- = 3.2 - (-7.5) = 10.7 \text{ V}$	[1]	
dV_{CE2}	$= \text{New}_V_{CE2} - \text{Ori}_V_{CE2} = 10.1 \text{ V}$	[0.5]	
dI_O	$= dV_{CE2} / R_O$	[1]	
	$= (10.1) / (250\text{k}) = 0.0404 \text{ mA}$	[0.5]	

Question:

Refer to **Figure 1**. All transistors are matched.

The circuit parameters are: $V^+ = 7.0 \text{ V}$ and $V^- = -7.0 \text{ V}$.

The transistor parameters are: $\beta = 100$, $V_{BE(\text{on})} = 0.6 \text{ V}$, and $V_A = 150 \text{ V}$.

(a) **Design** a two-transistor current source using all the parameters given above so that $I_{B2} = 7 \mu\text{A}$.

[4.5 marks]

(b) Find the **change in I_O** (i.e. dI_O) if $V_{C2} = 3.3 \text{ V}$.

[5.5 marks]

Show clearly all calculations as marks are given according to this.

Answer:

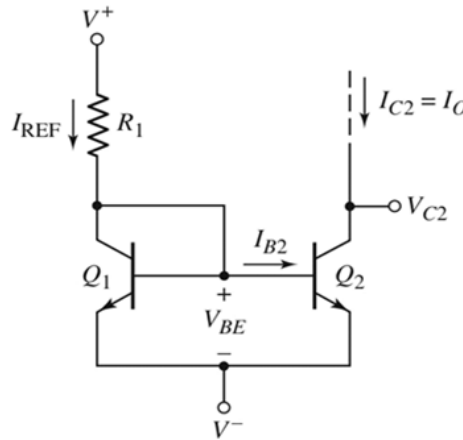


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$$i_E = i_B + i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

; Small signal

$I_O = I_{C2}$	$= \beta I_{B2}$ $= (100)(7\mu) = 0.7 \text{ mA}$	[1] [0.5]
I_{REF}	$= I_O (1 + 2/\beta)$ $= (0.7\text{m})(1 + 2/100) = 0.714 \text{ mA}$	[1] [0.5]
R_1	$= (V^+ - V_{BE} - V^-) / I_{REF}$ $= (7.0 - 0.6 - (-7.0)) / (0.714\text{m}) = 18.767 \text{ k}\Omega$	[1] [0.5]
R_O	$= r_{o2} = V_A / I_O$ $= (150) / (0.7\text{m}) = 214.28 \text{ k}\Omega$	[1] [0.5]
Ori_ V_{CE2}	$= V_{CE1} = V_{BE(\text{on})} = 0.6 \text{ V}$	[1]
New_ V_{CE2}	$= V_{C2} - V^- = 3.3 - (-7.0) = 10.3 \text{ V}$	[1]
dV_{CE2}	$= \text{New_} V_{CE2} - \text{Ori_} V_{CE2} = 9.7 \text{ V}$	[0.5]
dI_O	$= dV_{CE2} / R_O$ $= (9.7) / (214.28\text{k}) = 0.0453 \text{ mA}$	[1] [0.5]

$$\beta = g_m r_\pi$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

$$V_T = 26 \text{ mV}$$

Question:

Refer to **Figure 1**. All transistors are matched.

The circuit parameters are: $V^+ = 7.0 \text{ V}$ and $V^- = -7.0 \text{ V}$.

The transistor parameters are: $\beta = 120$, $V_{BE(\text{on})} = 0.6 \text{ V}$, and $V_A = 150 \text{ V}$.

(a) **Design** a two-transistor current source using all the parameters given above so that $I_{B2} = 7 \mu\text{A}$.

[4.5 marks]

(b) Find the **change in I_O** (i.e. dI_O) if $V_{C2} = 3.2 \text{ V}$.

[5.5 marks]

Show clearly all calculations as marks are given according to this.

Answer:

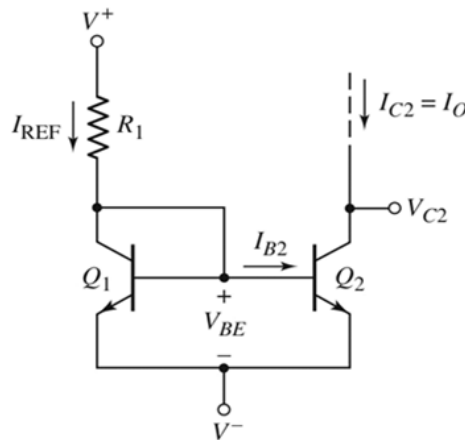


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;Small signal

$$\beta = g_m r_\pi$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

$$V_T = 26 \text{ mV}$$

$I_O = I_{C2}$	$= \beta I_{B2}$ $= (120)(7\mu) = 0.84 \text{ mA}$	[1] [0.5]
I_{REF}	$= I_O (1 + 2/\beta)$ $= (0.84\text{m})(1 + 2/120) = 0.854 \text{ mA}$	[1] [0.5]
R_1	$= (V^+ - V_{BE} - V^-) / I_{REF}$ $= (7.0 - 0.6 - (-7.0)) / (0.854\text{m}) = 15.691 \text{ k}\Omega$	[1] [0.5]
R_O	$= r_{o2} = V_A / I_O$ $= (150) / (0.84\text{m}) = 178.57 \text{ k}\Omega$	[1] [0.5]
Ori_ V_{CE2}	$= V_{CE1} = V_{BE(\text{on})} = 0.6 \text{ V}$	[1]
New_ V_{CE2}	$= V_{C2} - V^- = 3.2 - (-7.0) = 10.2 \text{ V}$	[1]
dV_{CE2}	$= \text{New_ } V_{CE2} - \text{Ori_ } V_{CE2} = 9.6 \text{ V}$	[0.5]
dI_O	$= dV_{CE2} / R_O$ $= (9.6) / (178.57\text{k}) = 0.0537 \text{ mA}$	[1] [0.5]

Question:

Refer to **Figure 1**. All transistors are matched.

The circuit parameters are: $V^+ = 7.5 \text{ V}$ and $V^- = -7.5 \text{ V}$.

The transistor parameters are: $\beta = 120$, $V_{BE(\text{on})} = 0.6 \text{ V}$, and $V_A = 150 \text{ V}$.

(a) **Design** a two-transistor current source using all the parameters given above so that $I_{B2} = 6 \mu\text{A}$.

[4.5 marks]

(b) Find the **change in I_O** (i.e. dI_O) if $V_{C2} = 3.3 \text{ V}$.

[5.5 marks]

Show clearly all calculations as marks are given according to this.

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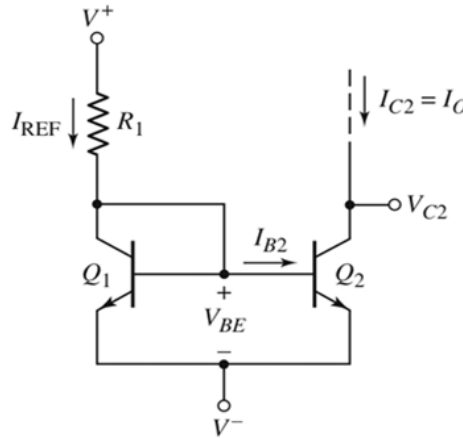


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$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_\pi = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

$$V_T = 26 \text{ mV}$$

$I_O = I_{C2}$	$= \beta I_{B2}$	[1]
	$= (120)(6\mu) = 0.72 \text{ mA}$	[0.5]
I_{REF}	$= I_O (1 + 2/\beta)$	[1]
	$= (0.72\text{m})(1 + 2/120) = 0.732 \text{ mA}$	[0.5]
R_1	$= (V^+ - V_{BE} - V^-) / I_{REF}$	[1]
	$= (7.5 - 0.6 - (-7.5)) / (0.732\text{m}) = 19.672 \text{ k}\Omega$	[0.5]
R_O	$= r_{o2} = V_A / I_O$	[1]
	$= (150) / (0.72\text{m}) = 208.33 \text{ k}\Omega$	[0.5]
Ori_ V_{CE2}	$= V_{CE1} = V_{BE(\text{on})} = 0.6 \text{ V}$	[1]
New_ V_{CE2}	$= V_{C2} - V^- = 3.3 - (-7.5) = 10.8 \text{ V}$	[1]
dV_{CE2}	$= \text{New_ } V_{CE2} - \text{Ori_ } V_{CE2} = 10.2 \text{ V}$	[0.5]
dI_O	$= dV_{CE2} / R_O$	[1]
	$= (10.2) / (208.33\text{k}) = 0.0489 \text{ mA}$	[0.5]