Name: **Dr JBO**

Student ID Number: Model Answer

Section:

Lecturer: Dr. Jamaludin Bin Omar

EEEB273 - Quiz 2

SEMESTER 2, ACADEMIC YEAR 2016/2017

Date: 8 November 2016 Time: 15 minutes

Question:

A Widlar current source circuit to be designed has the configuration shown in Figure 1. The circuit parameters are: $V^+ = +5.5 \text{ V}$ and $V^- = -5.5 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 80 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

(a) Design the Widlar current source circuit such that $I_{REF} = 1$ mA and $I_0 = 12$ μ A.

[4 marks]

(b) Find V_{BE2} . [2 marks]

(c) Find output resistance (R_0) of the Widlar current source in Figure 1 using given parameters, results from part (a) above, and the following formula. [4 marks]

$$R_O = r_{o2} \Big[1 + g_{m2} \Big(R_E || r_{\pi 2} \Big) \Big]$$

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5.5 - 0.6 - (-5.5)}{1\text{m}} = 10.4 \text{ k}\Omega \text{ [2]}$$

$$R_E = \frac{V_T}{I_O} \ln \left(\frac{I_{REF}}{I_O} \right) = \frac{0.026}{12} \ln \left(\frac{1\text{m}}{12} \right) = 9.58 \text{ k}\Omega$$
 [2]

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (12)(9.58k) = 0.485 \text{ V}$$
 [2]

(c)

$$g_{m2} = \frac{I_O}{V_T} = \frac{12\mu}{0.026} = 0.462 \text{ mA/V}$$
 [1]

$$r_{\pi^2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{12\mu} = 260 \text{ k}\Omega$$
 [1]

$$r_{o2} = \frac{V_A}{I_O} = \frac{80}{12\mu} = 6.67 \,\text{M}\Omega$$
 [1]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E \| r_{\pi 2} \right) \right]$$

$$R_O = (6.67 \text{M}) \left[1 + (0.462 \text{m}) \left(9.58 \text{k} \| 260 \text{k} \right) \right] = 35.1 \,\text{M}\Omega^{[1]}$$

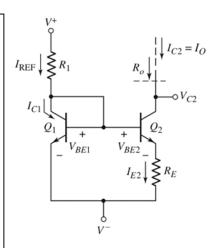


Figure 1

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Date: 8 November 2016 Time: 15 minutes Lecturer: Dr. Jamaludin Bin Omar

Question:

A Widlar current source circuit to be designed has the configuration shown in Figure 1. The circuit parameters are: $V^+ = +5.0 \text{ V}$ and $V^- = -5.0 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 80 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

(a) Design the Widlar current source circuit such that $I_{REF} = 1.2$ mA and $I_0 = 12$ μ A.

[4 marks]

(b) Find V_{BE2} .

[2 marks]

(c) Find output resistance (R_0) of the Widlar current source in Figure 1 using given parameters, results from part (a) above, and the following formula. [4 marks]

$$R_O = r_{o2} \Big[1 + g_{m2} \Big(R_E || r_{\pi 2} \Big) \Big]$$

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5 - 0.6 - (-5)}{1.2 \text{m}} = 7.83 \text{ k}\Omega$$
 [2]

$$R_E = \frac{V_T}{I_O} \ln \left(\frac{I_{REF}}{I_O} \right) = \frac{0.026}{12} \ln \left(\frac{1.2 \text{m}}{12} \right) = 9.98 \text{k}\Omega$$
 [2]

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (12)(9.98 \text{k}) = 0.48 \text{V}$$
 [2]

$$g_{m2} = \frac{I_O}{V_T} = \frac{12\mu}{0.026} = 0.462 \text{mA/V}$$
 [1]

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{12\mu} = 260\text{k}\Omega$$
 [1]

$$r_{o2} = \frac{V_A}{I_O} = \frac{80}{12\mu} = 6.67 \text{M}\Omega$$

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E || r_{\pi 2} \right) \right]$$
[1]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E \| r_{\pi 2} \right) \right]$$

$$R_O = (6.67 \text{M}) \left[1 + (0.462 \text{m}) \left(9.98 \text{k} \| 260 \text{k} \right) \right] = 36.2 \text{M}\Omega^{[1]}$$

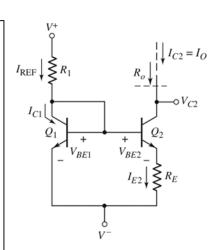


Figure 1

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Date: 8 November 2016 Time: 15 minutes

Question:

A Widlar current source circuit to be designed has the configuration shown in Figure 1. The circuit parameters are: $V^+ = +5.0 \text{ V}$ and $V^- = -5.0 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 100 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

(a) Design the Widlar current source circuit such that $I_{REF} = 1$ mA and $I_0 = 10$ μ A.

[4 marks]

(b) Find V_{BE2} .

[2 marks]

(c) Find output resistance (R_0) of the Widlar current source in Figure 1 using given parameters, results from part (a) above, and the following formula. [4 marks]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E || r_{\pi 2} \right) \right]$$

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5 - 0.6 - (-5)}{1\text{m}} = 9.40\text{k}\Omega$$
 [2]

$$R_E = \frac{V_T}{I_O} \ln \left(\frac{I_{REF}}{I_O} \right) = \frac{0.026}{10} \ln \left(\frac{1\text{m}}{10} \right) = 11.97 \text{k}\Omega$$
 [2]

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (10)(11.97 \text{k}) = 0.48 \text{V}$$
 [2]

(c)

$$g_{m2} = \frac{I_O}{V_T} = \frac{10\mu}{0.026} = 0.385 \text{mA/V}$$
 [1]

$$r_{\pi^2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{10\mu} = 312\text{k}\Omega$$
 [1]

$$r_{o2} = \frac{V_A}{I_O} = \frac{100}{10\mu} = 10.0 \text{M}\Omega$$
 [1]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E \| r_{\pi 2} \right) \right]$$

$$R_O = (10.0 \text{M}) \left[1 + (0.385 \text{m}) \left(11.97 \text{k} \| 312 \text{k} \right) \right] = 54.3 \text{M}\Omega^{[1]}$$

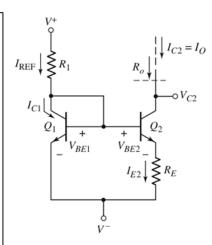


Figure 1

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Question:

A Widlar current source circuit to be designed has the configuration shown in Figure 1. The circuit parameters are: $V^+ = +5.5 \text{ V}$ and $V^- = -5.5 \text{ V}$. The transistor parameters are: $V_{BE1} = 0.6 \text{ V}$, $V_A = 100 \text{ V}$, and $\beta = 120$ (Therefore, we can assume that $I_C \approx I_E$).

(a) Design the Widlar current source circuit such that $I_{REF} = 1$ mA and $I_0 = 10$ μ A.

[4 marks]

(b) Find V_{BE2} .

[2 marks]

(c) Find output resistance (R_0) of the Widlar current source in Figure 1 using given parameters, results from part (a) above, and the following formula. [4 marks]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E || r_{\pi 2} \right) \right]$$

Answer:

(a)
$$R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{5.5 - 0.6 - (-5.5)}{1\text{m}} = 10.4\text{k}\Omega \quad [2]$$

$$R_E = \frac{V_T}{I_O} \ln \left(\frac{I_{REF}}{I_O} \right) = \frac{0.026}{10} \ln \left(\frac{1 \text{m}}{10} \right) = 11.97 \text{k}\Omega$$
 [2]

(b)
$$V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (10)(11.97 \text{k}) = 0.48 \text{V}$$
 [2]

(c)

$$g_{m2} = \frac{I_O}{V_T} = \frac{10\mu}{0.026} = 0.385 \text{mA/V}$$
 [1]

$$r_{\pi 2} = \frac{\beta V_T}{I_O} = \frac{(120)(0.026)}{10\mu} = 312\text{k}\Omega$$
 [1]

$$r_{o2} = \frac{V_A}{I_O} = \frac{100}{10\mu} = 10.0 \text{M}\Omega$$
 [1]

$$R_O = r_{o2} \left[1 + g_{m2} \left(R_E \| r_{\pi 2} \right) \right]$$

$$R_O = (10.0 \text{M}) \left[1 + (0.385 \text{m}) \left(11.97 \text{k} \| 312 \text{k} \right) \right] = 54.3 \text{M}\Omega^{[1]}$$

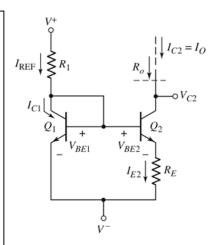


Figure 1