Name:

Student ID Number:

Section:

Lecturer: Dr Jamaludin / Dr Jehana Ermy/

Dr Azni Wati

Table Number:



College of Engineering

Department of Electronics and Communication Engineering

Test 2

SEMESTER 2, ACADEMIC YEAR 2016/2017

Subject Code : **EEEB273**

Course Title : Electronics Analysis & Design II

Date : **31 December 2016**

Time Allowed : 2 hours

Instructions to the candidates:

- 1. Write your Name and Student ID number. Indicate Lecturer for your section. Write your Table Number.
- 2. Write all your answers using pen. **DO NOT USE PENCIL** except for the diagram.
- 3. ANSWER ALL QUESTIONS.
- 4. WRITE YOUR ANSWER ON THIS QUESTION PAPER.

NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.



GOOD LUCK!



Question Number	Q1	Q2	Q3	Total
Marks				

Question 1 [30 marks]

For a MOSFET differential amplifier with cascode active load shown in Figure 1 the circuit parameters are: $V^+ = 5$ V, $V^- = -5$ V, and $I_Q = 1.2$ mA. Transistor parameters for N-MOSFET are: $V_{TN} = 0.7$ V, $k'_n = 130 \ \mu\text{A/V}^2$, $(W/L)_n = 100$ and $\lambda_n = 0.1$ V⁻¹; and the transistor parameters for P-MOSFET are: $V_{TP} = -0.8$ V, $k'_p = 35 \ \mu\text{A/V}^2$, $(W/L)_p = 200$ and $\lambda_p = 0.2$ V⁻¹.

- (a) **Find** the differential-mode voltage gain (A_d) of the differential amplifier with **cascode** active load. [14 marks]
- (b) Given that the common-mode voltage gain (A_{cm}) for the circuit is **-0.0025**. Calculate the Common-Mode Rejection Ratio (CMRR) in dB. [4 marks]
- (c) Calculate the maximum and minimum output voltage at v_o , i.e. $v_o(\max)$ and $v_o(\min)$. State any assumption used in the calculation. [12 marks]

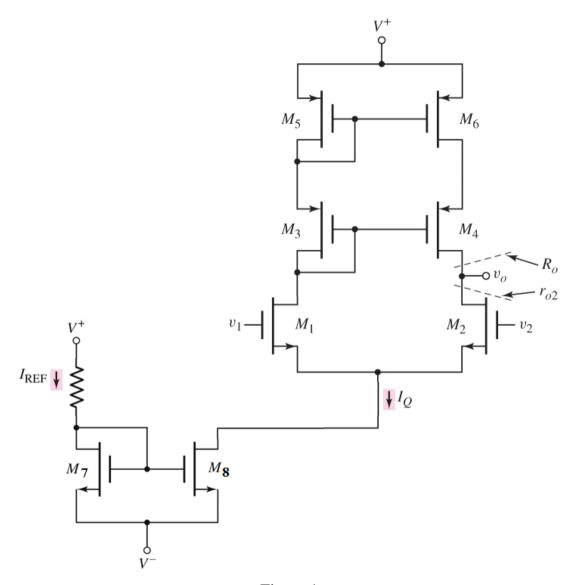


Figure 1

Answer for Question 1

Q1(a)

$$\begin{split} I_{D1} &= I_{Q}/2 = I_{D2} = I_{D3} = I_{D4} = I_{D5} = I_{D6} = 1.2 mA/2 = 0.6 mA \text{ [2]} \\ A_{d} &= g_{m2} \left(r_{o2} || R_{o} \right) \text{ [1]} \\ g_{m2} &= 2 \sqrt{K_{n} I_{D2}} = 2 \sqrt{\frac{k_{n}^{'}}{2} \left(\frac{W}{L} \right)_{2} I_{D2}} \\ g_{m2} &= 2 \sqrt{\left(\frac{130 \mu}{2} \right) (100) (0.6 m)} = 3.949 mA/V \text{ [2]} \\ r_{o2} &= \frac{1}{\lambda_{n} I_{D2}} = \frac{1}{(0.1) (0.6 m)} = 16.667 k\Omega \text{ [2]} \\ r_{o4} &= \frac{1}{\lambda_{p} I_{D4}} = \frac{1}{(0.2) (0.6 m)} = 8.333 k\Omega = r_{o6} \text{ [2]} \\ g_{m4} &= 2 \sqrt{K_{p} I_{D4}} = 2 \sqrt{\frac{k_{p}^{'}}{2} \left(\frac{W}{L} \right)_{4} I_{D4}} \\ g_{m4} &= 2 \sqrt{\left(\frac{35 \mu}{2} \right) (200) (0.5 m)} = 2.645 mA/V \text{ [2]} \\ R_{o} &= g_{m4} r_{o4} r_{o6} = (2.65 m) (8.333 k) (8.333 k) = 183.7 k\Omega \text{ [2]} \\ A_{d} &= (3.949 m) (16.667 k || 183.7 k) = 60.35 V/V \text{ [1]} \end{split}$$

Q1(b)

$$CMRR = \left| \frac{A_d}{A_{cm}} \right| = \left| \frac{60.35}{-0.0025} \right| = 24140 \quad [2]$$

$$CMRR_{dB} = 20 \log |CMRR| = 20 \log (24140) = 87.65 dB \quad [2]$$

Q1(c)

$$\begin{split} &V_{o}(\max) = V^{+} - V_{SD6}(sat) - V_{SD4}(sat) \quad [1] \\ &V_{SG4} = V_{SG6} \Rightarrow I_{D4} = \left(\frac{k_{p}^{'}}{2}\right) \left(\frac{W}{L}\right)_{4} \left(V_{SG4} + V_{TP}\right)^{2} \quad [1] \\ &0.6m = \left(\frac{35\mu}{2}\right) (200) \left(V_{SG4} + (-0.8)\right)^{2} \Rightarrow V_{SG4} = 1.214 \, \text{V} \quad [0.5] \\ &V_{SD4}(sat) = V_{SG4} + V_{TP} = 1.214 + (-0.8) = 0.414V = V_{SD6}(sat) \\ &\Rightarrow V_{o}(\max) = 5 - 2(0.414) = 4.172 \, \text{V} \quad [1] \\ &V_{o}(\min) = V^{-} + V_{DS8}(sat) + V_{DS2}(sat) \quad [1] \\ &V_{GS8} \Rightarrow I_{D8} = I_{Q} = \left(\frac{k_{n}^{'}}{2}\right) \left(\frac{W}{L}\right)_{8} \left(V_{GS8} - V_{TN}\right)^{2} \quad [1] \\ &1.2m = \left(\frac{130\mu}{2}\right) (100) \left(V_{GS2} - 0.7\right)^{2} \Rightarrow V_{GS8} = 1.13 \, \text{V} \quad [0.5] \\ &V_{DS8}(sat) = V_{GS8} - V_{TN} = 1.13 - 0.7 = 0.43 \, \text{V} \quad [1] \\ &V_{GS2} \Rightarrow I_{D2} = \left(\frac{k_{n}^{'}}{2}\right) \left(\frac{W}{L}\right)_{2} \left(V_{GS2} - V_{TN}\right)^{2} \quad [1] \\ &0.6m = \left(\frac{130\mu}{2}\right) (100) \left(V_{GS2} - 0.7\right)^{2} \Rightarrow V_{GS2} = 1.004 \, \text{V} \quad [0.5] \\ &V_{DS2}(sat) = V_{GS2} - V_{TN} = 1.004 - 0.7 = 0.304 \, \text{V} \quad [1] \end{split}$$

 \Rightarrow $V_a(\text{min}) = (-5) + 0.43 + 0.304 = -4.266 \text{ V}$

Question 2 [30 marks]

The circuit in **Figure 2** shows a simple multi-stage BJT op-amp, **consisting of 3 different stages**. It is given that $V_{BE}(\mathbf{on}) = 0.6 \text{ V}$, $V_A = 120 \text{ V}$, and $\beta = 120 \text{ for all transistors}$.

Assume the op-amp is ideal and $I_{C7} = I_Q = 40 \mu A$. Neglect base currents when calculating quiescent values.

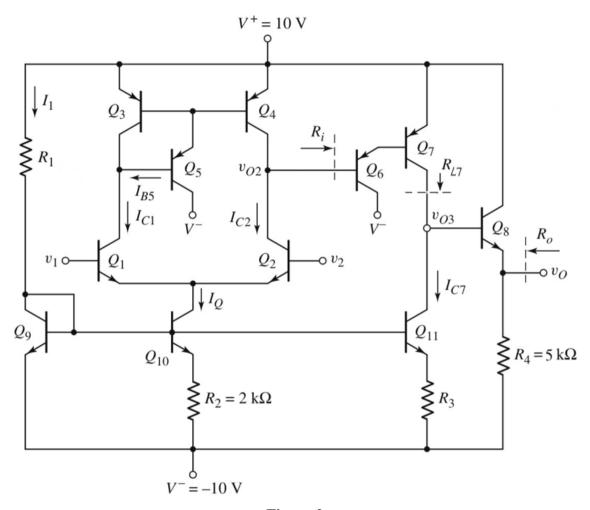


Figure 2

- (a) Calculate the input resistance (R_i) and the load resistance (R_{L7}) for the Darlington Pair as indicated in the Figure 2. [17 marks]
- (b) Calculate the <u>overall</u> differential-mode voltage gain of the op-amp, $A_d = v_O/v_d$. Consider the voltage gain of the gain stage, $A_2 = v_{O3}/v_{O2}$ is derived from the following relationships:

$$v_{O3} = I_{c7} (r_{o7} || R_{L7})$$

 $v_{O2} = I_{b6} R_i$ [13 marks]

Answer for Question 2

$$I_{C7} = I_O = 40 \mu A$$

$$I_{C6} = (\beta I_{E6})/(1+\beta) = (\beta I_{B7})/(1+\beta) = (\beta I_{C7}/\beta)/(1+\beta)$$
[1]
$$I_{C6} = I_{C7}/(1+\beta) = 40\mu/121 = 0.3305\mu A$$
[1]

$$r_{\pi 6} = \beta V_T / I_{C6} = (120x0.026) / 0.3305 \mu = 9.44 M\Omega$$
 [1]
 $r_{\pi 7} = \beta V_T / I_{C7} = (120x0.026) / 40 \mu = 78 k\Omega$ [1]

$$R_i = r_{\pi 6} + r_{\pi 7} (1 + \beta) = 9.44M + 78k(121) = 18.878M\Omega$$
 [2]

$$R_i = \frac{2(1+\beta)\beta V_T}{I_Q} = \frac{2x121x120x0.026}{40\mu} = 18.876M\Omega$$
 [Option = 6 marks]

$$R_{c11} = r_{o11}[1 + g_{m11}(r_{\pi 11} || R_3)]$$
 [1]

$$R_3 = R_2 = 2k\Omega \qquad [1]$$

$$r_{o11} = V_A / I_{C7} = 120/40 \mu = 3M\Omega$$
 [0.5]

$$r_{\sigma 11} = \beta V_T / I_{C7} = 120 \times 0.026 / 40 \mu = 78 k\Omega$$
 [05]

$$g_{m11} = I_{C7}/V_T = 40\mu/0.026 = 1.538mA/V$$
 [1]

$$R_{c11} = 3M[1 + (1.538m)(78k||2k)] = 1.99M\Omega$$
 [1]

[Total for $R_{c11} = 5$ marks]

$$I_{C8} = (v_O - V^-)/R_4 = (0 - (-10))/5k = 2mA$$
 [1]

$$R_{b8} = r_{\pi 8} + (1 + \beta)R_4 \qquad [1]$$

$$R_4 = 5k\Omega$$

$$r_{\pi 8} = \beta V_T / I_{C8} = 120 \times 0.026 / 2m = 1.56 k\Omega$$
 [1]

$$\rightarrow R_{b8} = 606.56k\Omega \qquad [1]$$

[Total for $R_{b8} = 4$ marks]

$$R_{L7} = R_{c11} \parallel R_{b8}$$
 [1]
 $\rightarrow R_{L7} = 1.99M \parallel 606.6k = 577.35k\Omega$ [1]

[Total for $R_{L7} = 2$ marks]

Q2(b)

From previous calculations:

$$I_{C7} = I_Q = 40 \mu A$$

$$R_i = 18.876 M\Omega$$

$$R_{L7} = 577.35 k\Omega$$

$$\begin{split} I_{C2} &= I_{C4} = I_Q / 2 = 20 \mu A & [1] \\ g_{m2} &= I_{C2} / V_T = 20 \mu / 0.026 = 0.769 m A / V & [1] \\ r_{o2} &= V_A / I_{C2} = 120 / 20 \mu = 6 M \Omega & [0.5] \\ r_{o4} &= V_A / I_{C4} = 120 / 20 \mu = 6 M \Omega & [0.5] \\ A_{d1} &= g_{m2} (r_{o2} \parallel r_{o4} \parallel R_i) & [1] \\ &\rightarrow A_{d1} = 0.769 m (2.588 M) = 1990 & [1] \end{split}$$

$$\begin{aligned} v_{o3} &= I_{c7}(r_{o7} \parallel R_{L7}) = (\beta I_{b7})(r_{o7} \parallel R_{L7}) = \beta (1+\beta)I_{b6}(r_{o7} \parallel R_{L7}) \end{aligned} [1] \\ v_{o2} &= I_{b6}R_{i} \\ A_{2} &= \frac{v_{o3}}{v_{o2}} = \frac{\beta (1+\beta)(r_{o7} \parallel R_{L7})}{R_{i}} \qquad [1] \\ r_{o7} &= V_{A} / I_{C7} = 120 / 40 \mu = 3M\Omega \qquad [1] \\ (r_{o7} \parallel R_{L7}) &= 3M \parallel 577.35k = 402.5k\Omega \\ \rightarrow A_{2} &= \frac{120x121x402.5k}{18.876M} = 309.6 \qquad [1] \end{aligned}$$

$$A_3 = 1$$
 [1]

Overall Gain,
$$Ad = A_{d1}xA_2xA_1$$
 [2]
 $\rightarrow A_d == 1990x309.6x1 = 616134$ [1]

Question 3 [40 marks]

- (a) Compare the performance of both Class A and Class B output stage in terms of power conversion efficiency, η . [5 marks]
- (b) **Describe** the **crossover distortion** experienced in **Class B** output stage and **explain** how the **crossover distortion** can be **eliminated**. [5 marks]
- (c) Consider the Class A emitter-follower circuit shown in Figure 3. Assume all transistors are matched with $V_{BE}(on) = 0.6 \text{ V}$, $V_{CE}(sat) = 0.2 \text{ V}$, and $V_A = \infty$. Neglect base currents.

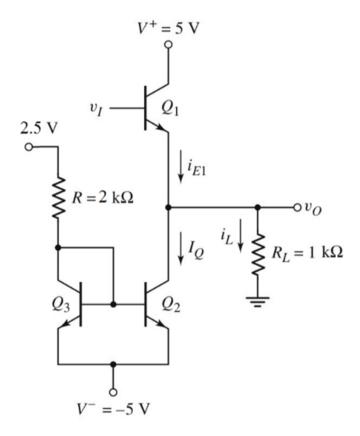


Figure 3

(i) **Find** the value of I_Q .

[5 marks]

- (ii) **Determine** the maximum and minimum values of **input voltage** for the circuit to operate in the linear region. [10 marks]
- (iii) For $v_0 = 0$ V, calculate the power dissipated in the transistor Q_1 and the power dissipated in the current source $(Q_2, Q_3, \text{ and } R)$. [8 marks]
- (iv) **Determine** the power conversion efficiency (η) for a symmetrical sine-wave output voltage (v_0) with peak value of **4 V**. [7 marks]

Answer for Question 3

- (a) Class A has low power conversion efficiency where its maximum efficiency is 25% [2.5] while Class B can reach up to 78.5% although suffering from cross-over distortion [2.5].
- (b) For a complementary push-pull output stage in Class B, both transistors are cut off [1] and v_O is 0 in the dead band portion [0.5]. A not perfect sinusoidal signal means that crossover distortion is produced by the dead band region [1.5]. Crossover distortion in Class B can be virtually eliminated by applying a small quiescent bias on each output transistor for a zero input signal. This creates a class-AB output stage. [2]
- (c) Class A emitter-follower circuit

(i)
$$I_Q = (V^+ - v_{BE}(on) - V^-)/R$$
 [2]
= $(2.5 - 0.6 + 5)/2k$ [2]
= 3.450 mA [1]

(ii)
$$v_I(max) = v_O(max) + v_{BE}(on)$$
 [2] $v_O(max) = V^+ - v_{CEI}(sat) = 5 - 0.2 = 4.8 \text{ V}$ [2] $So, v_I(max) = 4.8 + 0.6 = 5.4 \text{ V}$ [1]

$$v_I(min) = v_O(min) + v_{BE}(on)$$
 [2]
 $= [i_L(min)R_L + v_{BE}(on)]$ [1]
 $i_L(min) = -I_Q = -3.450 \text{ mA}$ [1]
 $v_I(min) = (-3.450 \text{m})(1 \text{k}) + 0.6 = -2.850 \text{ V}$ [1]

(iii)
$$P_{Q1} = I_{C1}.v_{CE1}$$
 [1]
= $I_{O}.v_{CE1} = (3.450\text{m})(5) = 17.25 \text{ mW}$ [1]

$$P_{Q2} = I_{C2}.v_{CE2}$$
 [1]
= $I_{Q}.v_{CE2} = (3.450\text{m})(0 - (-5)) = 17.25 \text{ mW}$ [1]

$$P_{Q3} = I_{C3}.v_{CE3}$$
 [1]
= $I_{O}.v_{BE}(on) = (3.450\text{m})(0.6) = 2.070 \text{ mW}$ [1]

$$P_R = I^2 R$$
 [1]
= $(3.450\text{m})^2 (2\text{k}) = \mathbf{0.0238 \text{ mW}}$

(iv) With peak value of 4 V.

Power conversion efficiency,
$$\eta = P_L / P_S \times 100\%$$
 [2]
 $P_L = 0.5(V_p)^2 / R_L = 0.5 (4)^2 / 1 \text{k} = \mathbf{8 mW}$ [2]
 $P_S = (V^+ - V^-) 2I_Q = (5 - (-5))(3.45 \text{m}) + (2.5 - (-5))(3.45 \text{m}) = \mathbf{60.375 mW}$ [2]
 $\eta = 8 \text{m} / 60.375 \text{m} \times 100\% = \mathbf{13.25\%}$ [1]

BASIC FORMULA FOR TRANSISTOR

BJT

$$i_C = I_S e^{v_{BE}/V_T}$$
; npn
 $i_C = I_S e^{v_{EB}/V_T}$; pnp
 $i_C = \alpha i_E = \beta i_B$
 $i_E = i_B + i_C$
 $\alpha = \frac{\beta}{\beta + 1}$

;Small signal

$$\beta = g_m r_{\pi}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

$$V_T = 26 \text{ mV}$$

MOSFET

; N - MOSFET

$$v_{DS}(\mathrm{sat}) = v_{GS} - V_{TN}$$

$$i_D = K_n [v_{GS} - V_{TN}]^2$$

$$K_n = \frac{k_n'}{2} \cdot \frac{W}{L}$$

; P - MOSFET

$$v_{SD}(\text{sat}) = v_{SG} + V_{TP}$$

$$i_D = K_p [v_{SG} + V_{TP}]^2$$

$$K_p = \frac{k_p}{2} \cdot \frac{W}{L}$$

;Small signal

$$g_m = 2\sqrt{K_? I_{DQ}}$$

$$r_o \cong \frac{1}{\lambda I_{DO}}$$