



**COLLEGE OF ENGINEERING
PUTRAJAYA CAMPUS
FINAL EXAMINATION**

SEMESTER 1 2017 / 2018

MODEL ANSWER

**PROGRAMME : Bachelor of Electrical & Electronics Engineering (Honours)
Bachelor of Electrical Power Engineering (Honours)**

SUBJECT CODE : EEEB273

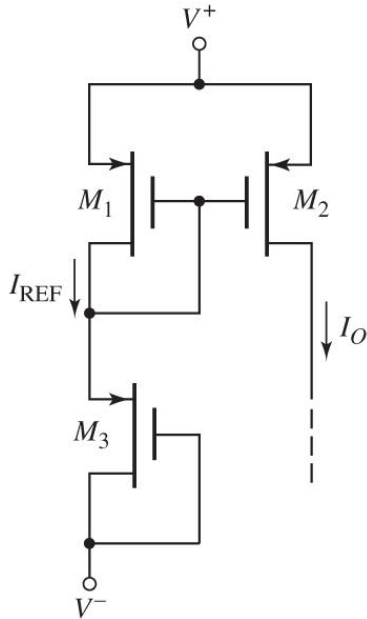
SUBJECT : ELECTRONIC ANALYSIS AND DESIGN II

DATE : September 2017

TIME : 3 hours

Answers to Question 1 [20 marks]

(a) The PMOS version of Figure 1 [5 marks]



- Correct placements of M_1 , M_2 and M_3 [2 marks]
- Labels for batteries, V^+ and V^- [1 mark]
- Labels for I_{REF} and I_O [2 marks]

(b) Find I_{REF} , I_O and $V_{SD2(sat)}$ [15 marks]

$$I_{REF} = \left(\frac{k'_p}{2}\right) \left(\frac{W}{L}\right)_1 (V_{SG1} + V_{TP})^2 \quad [2 \text{ marks}]$$

$$M_1 \text{ and } M_3: I_{REF} = \left(\frac{k'_p}{2}\right) \left(\frac{W}{L}\right)_1 (V_{SG1} + V_{TP})^2 = \left(\frac{k'_p}{2}\right) \left(\frac{W}{L}\right)_3 (V_{SG3} + V_{TP})^2 \quad [2 \text{ marks}]$$

$$\left(\frac{50}{2}\right) (15)_1 (V_{SG1} - 0.5)^2 = \left(\frac{50}{2}\right) (3)_3 (V_{SG3} - 0.5)^2 \dots (1) \quad [2 \text{ marks}]$$

$$\text{KVL: } V_{SG1} + V_{SG3} = 10 - V_{SG1} \dots (2) \quad [2 \text{ marks}]$$

$$\sqrt{\frac{15}{3}} (V_{SG1} - 0.5) = (10 - V_{SG1}) - 0.5 \quad [1 \text{ mark}]$$

$$3.236V_{SG1} = 10.618; V_{SG1} = \underline{3.281 \text{ V}} \quad [1 \text{ mark}]$$

$$\text{Subs back, } I_{REF} = \left(\frac{50}{2}\right) (15)_1 (3.281 - 0.5)^2 = \underline{2.900 \text{ mA}} \quad [2 \text{ marks}]$$

$$\text{So, } I_{REF} = I_O = 2.900 \text{ mA} \quad [1 \text{ mark}]$$

$$V_{SD2(sat)} = V_{SG2} + V_{TP} = 3.281 - 0.5 = \underline{2.781 \text{ V}} \quad [2 \text{ marks}]$$

Answers to Question 2 [20 marks]**Calculation of Ad [6 marks]**

$$I_Q = (80)/(20)I_{REF} = 4I_{REF} = 2\text{mA} \quad [1]$$

$$I_{D7} = I_{D8} = I_{D10} = I_Q/2 = 1\text{mA} \quad [0.5]$$

$$A_d = g_{m7}(r_{o8} \parallel r_{o10}) \quad [1]$$

$$g_{m7} = 2 \cdot \sqrt{K_{n7} \cdot I_{D7}} = (2) \sqrt{\frac{1}{2}(100\mu)(10)(1\text{m})} = 1.4142\text{m A/V} \quad [1]$$

$$r_{o8} = 1/\lambda_n \cdot I_{D8} = 1/(0.02)(1\text{m}) = 50\text{k}\Omega \quad [1]$$

$$r_{o10} = 1/\lambda_p \cdot I_{D10} = 1/(0.03)(1\text{m}) = 33.3\text{k}\Omega \quad [1]$$

$$A_d = 1.4142\text{m}(50\text{k} \parallel 33.3\text{k}) = 1.4142(20\text{k}) = 28.28 \quad [0.5]$$

Calculation of Ro [4 marks]

$$R_o = g_{m4} \cdot r_{o4} \cdot r_{o2} \quad [1]$$

$$g_{m4} = 2 \cdot \sqrt{K_{n4} \cdot I_{D4}} = (2) \sqrt{\frac{1}{2}(100\mu)(10)(2\text{m})} = 2\text{m A/V} \quad [1]$$

$$r_{o4} = 1/\lambda_n \cdot I_{D4} = 1/(0.02)(2\text{m}) = 25\text{k}\Omega = r_{o2} \quad [1]$$

$$R_o = (2\text{m})(25\text{k})(25\text{k}) = 1.25\text{ M}\Omega \quad [1]$$

Evaluation of Ro for CMRR [10 marks]

$$\text{CMRR} = |A_d / A_{cm}| \quad [2]$$

$$A_{cm} \text{ is inversely proportional to } R_o, A_{cm} \propto (1/R_o) \quad [2]$$

$$71\text{dB} \Rightarrow \text{CMRR} = 10^{71/20} = 3548 \quad [1]$$

$$80\text{dB} \Rightarrow \text{CMRR}_{\text{new}} = 10^{80/20} = 10000 \quad [1]$$

$$\text{Thus } R_{o_{\text{new}}} = (10000/3548)R_o = 2.82R_o \quad [1]$$

$$\text{i.e. } 2.82 \text{ is the factor of how much } R_o \text{ should } \underline{\text{increase}} \quad [2]$$

$$R_{o_{\text{new}}} = 2.82(1.25\text{M}\Omega) = 3.54\text{ M}\Omega \quad [1]$$

Answers to Question 3 [20 marks](a) Requires DC Analysis to find I_{C2}

$$I_{C2} = I_{C5}/2 = 0.5015 \text{ mA} \quad [1]$$

$$R_{id} = 2r_{\pi 2} = 2(\beta V_T / I_{C2}) = 2(200)(0.026)/0.5015 \text{ mA} = 20.74 \text{ k}\Omega \quad [3]$$

$$r_{o5} = V_A / I_{C5} = 80 / 1.003 \text{ mA} = 79.76 \text{ k}\Omega \quad [1]$$

$$R_{icm} = (1 + \beta)(R_{ocs}) = (201)(79.76 \text{ k}) = 16.03 \text{ M}\Omega \quad [2]$$

(b) $g_{m2} = I_{C2} / V_T = 0.5015 \text{ mA} / 0.026 \text{ V} = 19.29 \text{ mA/V}$ [1]

$$A_{d1} = (g_{m2} R_C) / 2 = (19.29 \text{ mA/V})(12 \text{ k}) / 2 = 115.7 \quad [2]$$

$$g_{m3} = I_{C3} / V_T = 1.886 \text{ mA} / 0.026 \text{ V} = 72.54 \text{ mA/V} \quad [1]$$

$$A_2 = g_{m3} R_{C2} = (72.54 \text{ mA/V})(4 \text{ k}) = 290.16 \quad [3]$$

Overall gain:

$$A_d = A_{d1} \times A_2 = (115.7)(290.16) = 33,580 \quad [2]$$

$$A_{cm} = A_{cm1} \times A_2 = (-0.0749)(290.16) = -21.73 \quad [1]$$

(c) $v_{o3} = A_d v_d + A_{cm} v_{cm}$

where

$$v_d = v_1 - v_2 = (2.015 \sin \omega t \text{ mV}) - (1.985 \sin \omega t \text{ mV}) = 0.03 \sin \omega t \text{ mV} \quad [2]$$

$$v_{o3} = (33,580)(0.03 \sin \omega t \text{ mV}) = 1.007 \sin \omega t \text{ V}. \quad [1]$$

If $A_{cm} = 0$, the diff-amp is ideal. The output is a pure amplification of the differential input.

Answers to Question 4 [25 marks]

Answers to Question 4(a) [15 marks]

Question 4(a)(i) [5 marks]

Figure 4(a) – (approximate) class-B output stage. [1]

Figure 4(b) – class-AB output stage. [1]

In class-AB, quiescent collector current I_{CQ} exists even for a zero input signal. Hence:

- 1) The average power supplied by each source and the average power dissipated in each transistor in class-AB are *larger* than class-B.
- 2) The η will be *less* than an approximate class-B.
- 3) The required power handling capability of the transistors in class-AB will be *slightly larger* than class-B. Since I_{CQ} is usually small compared to I_p , the increase in power dissipation is not great.

However, the advantage of eliminating crossover distortion greatly outweighs the disadvantage of reduced η and increased power dissipation. [3]

Question 4(a)(ii) [10 marks]

For $v_O = -8$ V,
 $i_L = V_O / R_L = (-8\text{V}) / (1 \text{ k}\Omega) = -8$ mA [1]

Therefore, Q_p is conducting and Q_n is OFF.

Approximation:

$i_{Cp} \approx |i_L| = 8$ mA [1]

$v_{EBp} = V_T \ln(i_{Cp} / I_S)$
 $= (0.026) \ln(8\text{m} / 4 \times 10^{-15}) = 0.7364$ V [1]

$v_{BE n} = V_{BB} - v_{EBp} = 1.35 - 0.7364 = 0.6136$ V [1]

$i_{Cn} = I_S \exp(v_{BE n} / V_T)$
 $= (4 \times 10^{-15}) \exp(0.6136 / 0.026) = 7.102 \times 10^{-5}$ A [1]

$i_{Cn} = i_{Cp} + i_L$ [1]

$i_{Cp} = i_{Cn} - i_L$ Recalculate i_{Cp}
 $= 7.102 \times 10^{-5} - (-8\text{m}) = 8.071$ mA [1]

$V_I = V_O + V_{BB}/2 - v_{EBp} = -8 + 1.35/2 - 0.7364 = -8.06$ V [1]

For Q_n :

$V_{CE n} = V_{CC} - V_O = 10 - (-8) = 18$ V [0.5]

$P_{Qn} = i_{Cn} V_{CE n} = (7.102 \times 10^{-5})(18) = 1.278$ mW [0.5]

For Q_p :

$V_{EC p} = V_O - (-V_{CC}) = (-8) - (-10) = 2$ V [0.5]

$P_{Qp} = i_{Cp} v_{EC p} = (8.071\text{m})(2) = 16.14$ mW [0.5]

Answers to Question 4(b) [10 marks]

To calculate I_{C16} , need to determine I_{C12} and I_{C13B}

$$I_{C12} = [V^+ - V - V_{EB12} - V_{BE11}] / R_5 = [10 - 2(0.65)] / 40k = 0.2175mA \quad [2]$$

$$I_{C13B} = 0.75 I_{C12} = (0.75)(0.2175mA) = 0.1631 mA \quad [1]$$

$$I_{C16} \cong I_{E16} = I_{B17} + (V_{BE17}/R_9) = I_{C17} / \beta + (V_{BE17}/R_9) \quad [3]$$

$$I_{C17} = I_{C13B} = 0.1631 mA \quad [1]$$

$$I_{C16} = (0.1631mA/200) + (0.65/50k) = 0.8155\mu + 13\mu = 13.82 \mu A \quad [2]$$

Either logical reason: [1]

Example: *shifts dc voltage level at output, increases bias current, increase out resistance thus increases small signal voltage gain of the circuit.*

Answers to Question 5 [15 marks]

Question 5(a) [5 marks]

$$\begin{aligned} v_O &= (-R_4/R_3)v_{O1} & [1] \\ v_{O1} &= (R_2/(R_1+R_2))v_1 & [1] \\ v_O &= (-R_4/R_3) (R_2/(R_1+R_2))v_1 & [1] \\ v_O/v_1 &= -(R_4/R_3) (R_2/(R_1+R_2)) & [1] \\ &= -[(75k/80k)(100k/150k)] = 0.625 \text{ V/V} & [1] \end{aligned}$$

Question 5(b)(i) [7 marks]

$$i_1 = \frac{v_{I1} - v_{I2}}{R_{1f} + R_{1POT}} \quad [1]$$

$$v_{O1} = v_{I1} + i_1 R_2 = \left(1 + \frac{R_2}{R_{1f} + R_{1POT}}\right) v_{I1} - \frac{R_2}{R_{1f} + R_{1POT}} v_{I2} \quad [2]$$

$$v_{O2} = v_{I2} - i_1 R_2 = \left(1 + \frac{R_2}{R_{1f} + R_{1POT}}\right) v_{I2} - \frac{R_2}{R_{1f} + R_{1POT}} v_{I1} \quad [2]$$

$$v_O = \frac{R_4}{R_3} (v_{O2} - v_{O1})$$

$$v_O = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_{1f} + R_{1POT}}\right) (v_{I2} - v_{I1}) \quad [2]$$

Question 5(b)(ii) [3 marks]

$$A_v = \frac{v_O}{(v_{I2} - v_{I1})} = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_{1f} + R_{1POT}}\right) \quad [1]$$

$$A_v = \frac{2.5R_3}{R_3} \left(1 + \frac{2(495k)}{15k + 40k}\right) = 47.5 \text{ V/V} \quad [1]$$

$$v_O = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_{1f} + R_{1POT}}\right) (v_{I2} - v_{I1})$$

$$v_O = A_v (v_{I2} - v_{I1}) = (47.5)(0.115 - 0.090) = 1.1875 \text{ V} \quad [1]$$