



**College of Engineering**  
Department of Electronics and Communication Engineering

**Test 1 (Solution)**

**SEMESTER 1, ACADEMIC YEAR 2017/2018**

Subject Code : **EEEEB273**  
Course Title : **Electronics Analysis & Design II**  
Date : **8 July 2017**  
Time Allowed : **2 hours**

**Instructions to the candidates:**

1. Write your Name and Student ID Number. Indicate your Section Number and Lecturer's Name. Write also your Table Number.
2. **Write all your answers using pen. DO NOT USE PENCIL** except for the diagram.
3. **ANSWER ALL QUESTIONS. Show clearly** all your calculations. Every value **must** be written with its correct Unit.
4. **WRITE YOUR ANSWER ON THIS QUESTION PAPER.**

**NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.**

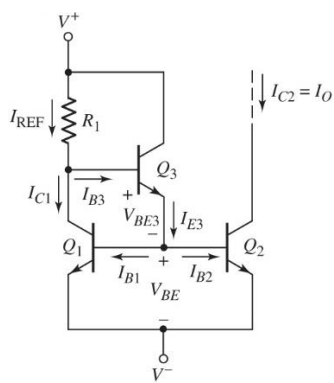
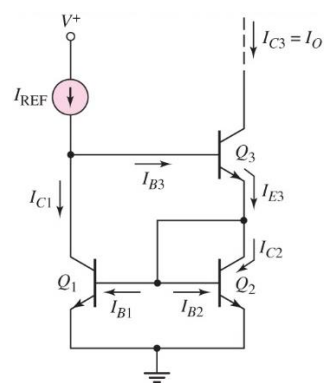


**GOOD LUCK!**



Question Number	Q1	Q2	Q3	Q4	Total
Marks					

**Answers for Question 1**

<p>(i) <u>Three transistor current source</u></p>  <p>Placements of <math>Q_1</math>, <math>Q_2</math> and <math>Q_3</math> [2 marks]          Batteries <math>V^+</math> and <math>V^-</math> labels [2 marks]          Currents <math>I_{REF}</math> and <math>I_O</math> labels [2 marks]</p>	<p><u>Wilson current source</u></p>  <p>Placements of <math>Q_1</math>, <math>Q_2</math> and <math>Q_3</math> [2 marks]          Batteries <math>V^+</math> and <math>V^-</math> labels [2 marks]          Currents <math>I_{REF}</math> and <math>I_O</math> labels [2 marks]</p>
<p>(ii) Both three-transistor and Wilson current sources have an increased stability [1.5 marks] with smaller <math>I_O</math> change [1.5 marks].</p>	
<p>(iii) For Widlar current source:          Assuming that both <math>Q_1</math> and <math>Q_2</math> are identical,  <math>I_{REF} \cong I_{C1} = I_S e^{\frac{V_{BE1}}{V_T}}</math> [1 mark]  <math>I_O \cong I_{C2} = I_S e^{\frac{V_{BE2}}{V_T}}</math> [1 mark]          Solving the <math>V_{BE}</math> voltages,  <math>V_{BE1} = V_T \ln\left(\frac{I_{REF}}{I_S}\right)</math> and <math>V_{BE2} = V_T \ln\left(\frac{I_O}{I_S}\right)</math> [2 marks]          Combining the equations for VBEs, <math>V_{BE1} - V_{BE2} = V_T \ln\left(\frac{I_{REF}}{I_S}\right) - V_T \ln\left(\frac{I_O}{I_S}\right)</math> [1 mark]          Hence, <math>V_{BE1} - V_{BE2} = V_T \ln\left(\frac{I_{REF}}{I_O}\right)</math> [1 mark]          From the circuit, <math>V_{BE1} - V_{BE2} = I_{E2} R_E \cong I_O R_E</math> [2 marks]          Combining the equations, <math>I_O R_E = V_T \ln\left(\frac{I_{REF}}{I_O}\right)</math> [2 marks]</p>	
<p>(iv) <math>R_1 = \frac{V^+ - V_{BE1} - V^-}{I_{REF}} = \frac{3 - 0.6 - (-3)}{0.1m} = 54.00 \text{ k}\Omega</math> [1.5, 1, 1 marks]  <math>R_E = \frac{V_T}{I_O} \ln\left(\frac{I_{REF}}{I_O}\right) = \frac{0.026}{0.02m} \ln\left(\frac{0.1m}{0.02m}\right) = 2.092 \text{ k}\Omega</math> [1.5, 1, 1 marks]  <math>V_{BE2} = V_{BE1} - I_O R_E = 0.6 - (0.02m)(2.092k) = 0.5582 \text{ V}</math> [1, 1, 1 marks]</p>	

**Answers for Question 2**

## Question 2(a)

$$V_{DS2}(\text{min}) = V_{D2} - V_{S2} = -2.1 - (-3) = \underline{0.9V} = \underline{V_{DS2}(\text{sat})} \quad [2]$$

$$V_{DS2}(\text{sat}) = V_{GS2} - V_{TN}$$

$$V_{GS2} = V_{DS2}(\text{sat}) + V_{TN} = 0.9 + 0.5 = \underline{1.4V} \quad [1]$$

$$\text{From circuit, } \underline{V_{GS1} = V_{GS2} = 1.4V} \quad [1]$$

$$I_o = I_{D2} = \left(\frac{1}{2}\mu_n C_{ox}\right)(W/L)_2 (V_{GS2} - V_{TN})^2 \\ = (50 \mu)(35)(1.4-0.5)^2 = \underline{1.418mA} \quad [2]$$

$$I_{REF} = I_{D1} = \left(\frac{1}{2}\mu_n C_{ox}\right)(W/L)_1 (V_{GS1} - V_{TN})^2 \\ = (50 \mu)(20)(1.4-0.5)^2 = \underline{0.810mA} \quad [1]$$

$$I_{D3} = I_{D4} = I_{REF} = 0.810mA \quad [1]$$

$$I_{D3} = 0.810mA = \left(\frac{1}{2}\mu_n C_{ox}\right)(W/L)_3 (V_{GS3} - V_{TN})^2 \\ = (50 \mu)(5)(V_{GS3}-0.5)^2$$

$$\underline{V_{GS3} = 2.3V} \quad [2]$$

$$I_{D4} = 0.810mA = \left(\frac{1}{2}\mu_p C_{ox}\right)(W/L)_4 (V_{SG4} + V_{TP})^2 \\ = (20 \mu)(10)(V_{SG4} + (-0.55))^2$$

$$\underline{V_{SG4} = 2.562V} \quad [2]$$

## Question 2(b)

$$dI_o = dV_{D2}/R_o \quad [1]$$

$$dV_{D2} = 0.4 - (-1.6) = \underline{2V} \quad [1]$$

$$R_o = r_{o2}$$

$$r_{o2} = 1/(\lambda_n)(I_{D2}) = 1/(0.02)(1.418mA) = \underline{35.26k\Omega} \quad [2]$$

$$dI_o = 2/35.26k = \underline{56.72\mu A} \quad [1]$$

## Question 2(c)

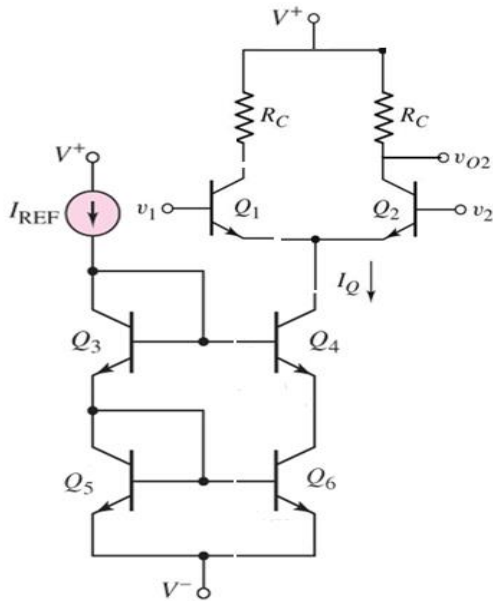
$$I_o' = I_o + dI_o \quad [1]$$

$$= 1.418mA + 56.72\mu A$$

$$= \underline{1.475mA} \quad [2]$$

**Answers for Question 3**

(a)



Cascode CS	[2]
Supply connections	[1]
Output and reference connection of CS	[2]

- (b)  $I_{C2} = I_Q / 2 = 0.5\text{m} / 2 = 0.25\text{ mA}$  [2]  
 $R_C = [V^+ - v_{O2}] / I_{C2}$  [2]  
 $= [12 - 0.4] / 0.25\text{m} = 46.4\text{k}\Omega$  [2]
- (c)  $v_d = v_1 - v_2$  [2]  
 $v_d = (250 - 150) \sin \omega t \mu\text{V} = 100 \sin \omega t \mu\text{V}$  [2]
- (d)  $v_{cm} = (v_1 + v_2) / 2$  [2]  
 $= [(250 + 150) / 2] \sin \omega t \mu\text{V} = 200 \sin \omega t \mu\text{V}$  [2]
- (e)  $v_o = A_d v_d + A_{cm} v_{cm}$  [2]  
 $v_o = (223) 100 \sin \omega t \mu\text{V} + (-10)(200 \sin \omega t \mu\text{V})$  [2]  
 $= (22.3\text{m} - 2\text{m}) \sin \omega t \text{V} = 20.3 \sin \omega t \text{mV}$  [2]

**Answers for Question 4**

$$V_o = \frac{\beta R_C}{2(r_\pi + R_B)} V_d - \frac{\beta R_C}{r_\pi + R_B + 2(1 + \beta)R_o} V_{cm}$$

$$R_B = 0$$

$$\Rightarrow V_o = \frac{\beta R_C}{2r_\pi} V_d - \frac{\beta R_C}{r_\pi + 2(1 + \beta)R_o} V_{cm} \quad [2]$$

$$V_o = A_d V_d + A_{cm} V_{cm} \quad [2]$$

$$A_d = \frac{\beta R_C}{2r_\pi} = \frac{g_m r_\pi R_C}{2r_\pi} = \frac{g_m R_C}{2} \quad [2]$$

$$g_m = \frac{I_Q}{2V_T} = \frac{(0.8\text{m})}{2(0.026)} = 15.384 \text{ mA/V} \quad [2]$$

$$r_\pi = \frac{2V_T \beta}{I_Q} = \frac{2(0.026)(100)}{(0.8\text{m})} = 6.5 \text{ k}\Omega \quad [2]$$

$$\Rightarrow A_d = \frac{g_m R_C}{2} = \frac{I_{CQ} R_C}{2V_T} = \frac{I_Q R_C}{2(2V_T)} = \frac{I_Q R_C}{4V_T} = \frac{(0.8\text{m})(12\text{k})}{4(0.026)} = 92.3 \quad [2]$$

$$A_{cm} = \frac{-\beta R_C}{r_\pi + 2(1 + \beta)R_o} \quad [2]$$

$$\Rightarrow A_{cm} = \frac{-\beta R_C}{r_\pi + 2(1 + \beta)R_o} = \frac{-g_m R_C}{1 + \frac{2(1 + \beta)R_o g_m}{\beta}} = \frac{-\frac{I_Q}{2V_T} R_C}{1 + \frac{2(1 + \beta)R_o}{\beta} \frac{I_Q}{2V_T}} = -0.237 \quad [2]$$

$$CMRR = \left| \frac{A_d}{A_{cm}} \right| = \left| \frac{92.3}{-0.237} \right| = 389 \quad [4]$$