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Table Number:



College of Engineering
Department of Electronics and Communication Engineering

Test 1 – Model Answers

SEMESTER 1, ACADEMIC YEAR 2018/2019

Subject Code : **EEEB273**
Course Title : **Electronics Analysis & Design II**
Date : **7 July 2018**
Time Allowed : **2 hours**

Instructions to the candidates:

1. Write your Name and Student ID Number. Indicate your Section Number and Lecturer's Name. Write also your Table Number.
2. **Write all your answers using pen. DO NOT USE PENCIL** except for the diagram.
3. **ANSWER ALL QUESTIONS. Show clearly** all your calculations. Every value **must** be written with its correct Unit.
4. **WRITE YOUR ANSWER ON THIS QUESTION PAPER.**

NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.

☺ **GOOD LUCK!** ☺

Question Number	Q1 (a)	Q1 (b)	Q2 (a)	Q2 (b)	Q3 (a)	Q3 (b)	Q4 (a-c)	Q4 (d)	Total
Marks									

QUESTION 1 [35 marks]

Answers for Question 1

Answers for Question 1(a)

- (i) Better approximation of I_O to I_{REF} for circuit using same transistors [2]
- (ii) Higher output resistance by a factor of $\beta/2$ [2]
- (iii) Higher output resistance by a factor of 2 [2]
- (iv) Higher output resistance by a factor of $(1 + g_m R'_E)$ [2]
 Using smaller resistors in the circuit [2]
 Can have different values for I_O and I_{REF} where I_O is smaller than I_{REF} [2]
For (iv) → Can use any two answers above, total 4 marks.

Answers for Question 1(b)

- (i)
 - $I_{B1} = I_{B2}$ [1.5]
 - $I_O = I_{C2} = \beta I_{B2}$ $I_{B2} = I_O / \beta$ [1.5]
 - $I_{C1} = I_{C2}$ $I_{C1} = I_O$ [1.5]
 - $I_{E3} = 2 I_{B2} + V_{BE} / R_2$ [1.5]
 - $I_{B3} = I_{E3} / (1 + \beta)$ [1.5]
 - $= (2 I_{B2}) / (1 + \beta) + (V_{BE}) / ((1 + \beta) R_2)$
 - $= (2 I_O) / (\beta(1 + \beta)) + (V_{BE}) / ((1 + \beta) R_2)$ [1.5]
 - $I_{REF} = I_{C1} + I_{B3}$ [1.5]
 - $= I_O + (2 I_O) / (\beta(1 + \beta)) + (V_{BE}) / ((1 + \beta) R_2)$ [1.5]
 - $I_{REF} - (V_{BE}) / ((1 + \beta) R_2) = I_O + (2 I_O) / (\beta(1 + \beta))$ [1.5]
 - $= I_O [1 + 2 / (\beta(1 + \beta))]$

 - $I_{REF} - \frac{V_{BE}}{(1 + \beta) R_2} = I_O \left(1 + \frac{2}{\beta(1 + \beta)} \right)$ [1.5]

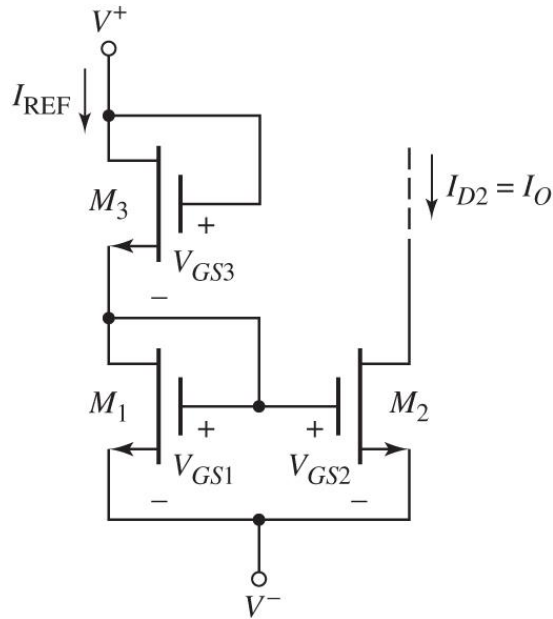
- (ii)
 - $I_{REF} = I_O (1 + 2 / (\beta(1 + \beta))) + (V_{BE}) / ((1 + \beta) R_2)$ [2]
 - $= (0.70\text{m})(1 + 2 / (80 \times 81)) + (0.7) / (81 \times 10\text{k})$ [2]
 - $= 0.700216\text{m} + 0.000864\text{m} = 0.7011\text{ mA}$ [1]

 - $R_1 = (V^+ - 2V_{BE(\text{on})} - 0) / I_{REF}$ [2]
 - $= (10 - 2(0.7)) / (0.7011\text{m})$ [2]
 - $= 12.27\text{ k}\Omega$ [1]

QUESTION 2 [20 marks]

Answers for Question 2

Q2(a)



Placement of M_1 , M_2 and M_3 [5]

Currents I_{REF} and I_O [3]

Power supplies V^+ and V^- [2]

Answers for Question 2 (Continued)

Q2(b) Using the equation, $V_{DS}(sat) = V_{GS} - V_{TN}$

$$V_{DS2}(sat) = V_{GS2} - V_{TN}$$

$$V_{GS2} = V_{DS2}(sat) + V_{TN} \quad [2]$$

$$= 0.6 + 0.4 = \underline{\mathbf{1.0\ V}} \quad [1]$$

From the RHS; solve for $(W/L)_2$ using the equation given.

$$\left(\frac{W}{L}\right)_2 = \frac{I_O}{\left(\frac{k'_n}{2}\right)(V_{GS2} - V_{TN})^2} \quad [1]$$

$$= (50\mu)/(120\mu/2)[1-0.4]^2$$

$$= \underline{\mathbf{2.315}} \quad [0.5]$$

$$\text{Since } V_{GS1} = V_{GS2} = 1V \quad [1]$$

Solve for

$$\left(\frac{W}{L}\right)_1 = \frac{I_{REF}}{\left(\frac{k'_n}{2}\right)(V_{GS1} - V_{TN})^2} \quad [1]$$

$$= (100\mu)/(120\mu/2)[1-0.4]^2$$

$$= \underline{\mathbf{4.63}} \quad [0.5]$$

For the LHS; solve for V_{GS3} .

$$V_{GS3} = V^+ - V_{GS1} - V \quad [1]$$

$$= 2.5 - 1 = 1.5\ V \quad [0.5]$$

Solve for

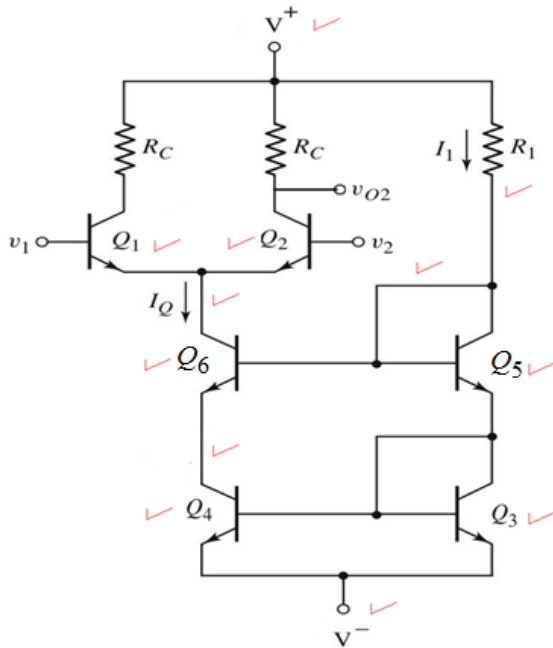
$$\left(\frac{W}{L}\right)_3 = \frac{I_{REF}}{\left(\frac{k'_n}{2}\right)(V_{GS3} - V_{TN})^2} \quad [1]$$

$$= (100\mu)/(120\mu/2)[1.5 - 0.4]^2$$

$$= \underline{\mathbf{1.377}} \quad [0.5]$$

QUESTION 3 [25 marks]

Answers for Question 3(a)



Marking:	
Correct differential amplifier with Rc and inputs	[1]
E1/E2 to C6 (or C4) connection (IQ)	[1]
V+ and V-	[1]
Correct cascode current source connection	[1]
Correct Iref/I1 side with diode connected transistors	[1]

Answers for Question 3(b)

(b)

$$V_{CE4} = V^+ - I_{C4}R_C - V_E$$

$$I_{C4} = \frac{V^+ - V_{CE4} - V_E}{R_C} \quad [2]$$

$$I_{C4} = \frac{10 - (1.8) - (-0.7)}{10k} = 0.89 \text{ mA} \quad [2]$$

$$I_{E4} = \frac{1 + \beta}{\beta} I_{C4} \quad [2]$$

$$I_{E4} = \left(\frac{41}{40}\right) (0.89 \text{ mA}) = 0.91225 \text{ mA} \quad [2]$$

$$I_{C2} = 2I_{E4} \quad [2]$$

$$I_{C2} = 2(0.91225 \text{ mA}) = 1.8245 \text{ mA} \quad [2]$$

$$I_1 = \left(1 + \frac{2}{\beta(1 + \beta)}\right) (I_{C2}) \quad [2]$$

$$I_1 = \left(1 + \frac{2}{(40)(41)}\right) (1.8245 \text{ mA}) = 1.826725 \text{ mA} \quad [2]$$

$$R_1 = \frac{V^+ - 2V_{BE} - V^-}{I_1} \quad [2]$$

$$R_1 = \frac{10 - 2(0.7) + 10}{1.826725 \text{ mA}} = 10.182 \text{ k}\Omega \quad [2]$$

QUESTION 4 [20 marks]

Answers for Question 4

Q4(a) Calculate the value of resistor R_C . [3 marks]

$$V_{RC} = V_+ - V_{o2} = I_{C2}R_C \quad [1]$$

$$I_{C2} = \frac{I_Q}{2} = 200\mu/2 = 100\mu \quad [1]$$

$$V_{RC} = 10 - 5 = 5V$$

$$\text{So } R_C = 5/100\mu = 50k\Omega \quad [1]$$

Q4(b) Find the differential voltage gain (A_d) and common-mode voltage gain (A_{cm}) for one-sided output [10 marks]

$$A_d = \frac{g_{m1}R_C}{2} \quad [1]$$

$$g_{m1} = \frac{I_{C1}}{V_T}, I_{C1} = I_{C2} = 100\mu \quad [1]$$

$$g_{m1} = \frac{100\mu}{26m} = 3.846 \text{ mA/V} \quad [1]$$

$$A_d = \frac{(3.846m)(50k)}{2} = 96.15 \text{ V/V} \quad [1]$$

Version 1

$$\text{Given CMRR(dB)} = 85\text{dB} = 20 \text{ Log CMRR} \quad [1]$$

$$\text{Therefore CMRR} = 10^{(85/20)} = 17\,783 \quad [1]$$

$$\text{CMRR} = A_d/|A_{cm}| \quad [2]$$

$$\text{So } |A_{cm}| = A_d/\text{CMRR} = 96.15 / 17783 = 5.407 \times 10^{-3} \quad [2]$$

Version 2

$$A_{cm} = - \frac{g_m R_C}{1 + \frac{2(1+\beta)R_o}{r_{\pi} + R_B}} \quad [2]$$

$$R_o = r_{o4}(1 + g_{m4}(r_{\pi 4} || R_2)) \quad [0.5]$$

$$r_{o4} = V_{A4}/I_Q = 200/200\mu = 1M\Omega \quad [0.5]$$

$$g_{m4} = I_Q/V_T = 200\mu/26m = 7.69\text{mA/V} \quad [0.5]$$

$$r_{\pi 4} = \beta_4 V_T/I_Q = 500(26m)/200\mu = 65k\Omega \quad [0.5]$$

$$R_o = 15.23M\Omega \quad [0.5]$$

$$r_{\pi 1} = \frac{\beta_1 V_T}{I_{C1}} = \frac{(200)(0.026)}{100\mu} = 52 \text{ k}\Omega \quad [0.5]$$

$$A_{cm} = - \frac{(3.848m)(50k)}{1 + \frac{2(1 + 200)15.23M}{52k}} = - 1.634 \times 10^{-3} \quad [1]$$

Q4(c) Determine the differential-mode input resistance R_{id} and the common-mode input resistance

R_{icm} [5 marks]

$$R_{id} = 2r_{\pi 1} \quad [0.5]$$

$$r_{\pi 1} = \frac{\beta_1 V_T}{I_{C1}} = \frac{(200)(0.026)}{100\mu} = 52 \text{ k}\Omega \quad [0.5]$$

$$\text{So } R_{id} = 2(52\text{k}) = 104 \text{ k}\Omega \quad [0.5]$$

$$R_{icm} = (1+B)[R_o] \quad [0.5]$$

$$R_o = r_{o4}(1+g_{m4}(r_{\pi 4}||R_2)) \quad [0.5]$$

$$r_{o4} = V_{A4}/I_Q = 200/200\mu = 1\text{M}\Omega \quad [0.5]$$

$$g_{m4} = I_Q/V_T = 200\mu/26\text{m} = 7.69\text{mA/V} \quad [0.5]$$

$$r_{\pi 4} = \beta_4 V_T/I_Q = 500(26\text{m})/200\mu = 65\text{k}\Omega \quad [0.5]$$

$$R_o = 15.23\text{M}\Omega \quad [0.5]$$

$$R_{icm} = (1+200)(15.23\text{M}) = 3.06 \text{ G}\Omega \quad [0.5]$$

Q4(d) If the circuit is modified such that resistor R_2 is zero, will this improve the common mode rejection performance of the differential amplifier? Justify your answer. [2 marks]

If R_2 is zero, the current source is now the simple 2 transistor current source, [1/2]

which has lower output resistance R_o than the Widlar current source. [1/2]

This will cause the value of common mode voltage gain A_{cm} to increase, [1/2]

hence CMRR will decrease. Hence the performance will worsen. [1/2]