

**COLLEGE OF ENGINEERING
PUTRAJAYA CAMPUS
FINAL EXAMINATION**

SEMESTER 2 2018 / 2019

MODEL ANSWERS

PROGRAMME	: Bachelor of Electrical & Electronics Engineering (Honours) Bachelor of Electrical Power Engineering (Honours)
SUBJECT CODE	: EEEB273/EEEB2014
SUBJECT	: ELECTRONIC ANALYSIS AND DESIGN II
DATE	: January/February 2019
TIME	: 3 hours

INSTRUCTIONS TO CANDIDATES:

1. This paper contains **FIVE** (5) questions in **TEN** (10) pages.
2. Answer **ALL** questions.
3. Write **all** answers in the answer booklet provided. Use **pen** to write your answer.
4. Write answer to different question on a **new page**.

THIS QUESTION PAPER CONSISTS OF **TEN** (10) PRINTED PAGES INCLUDING THIS COVER PAGE.

Question 1 [20 marks]

Answers:

Q1(a) Calculate the percentage change in output current I_O . [8 marks]

$$R_O = r_{O2}[1 + g_{m2}(r_{\pi2} || R_E)] \quad [1]$$

$$r_{O2} = \frac{V_A}{I_O} = \frac{200}{20\mu} = 12.5 \text{ M}\Omega \quad [0.5]$$

$$g_{m2} = \frac{I_O}{V_T} = \frac{20\mu}{26\text{m}} = 0.7692 \text{ mA/V} \quad [0.5]$$

$$r_{\pi2} = \frac{\beta V_T}{I_O} = \frac{200(26\text{m})}{20\mu} = 260 \text{ k}\Omega \quad [0.5]$$

$$R_E = \frac{V_T}{I_O} \ln\left(\frac{I_{REF}}{I_O}\right) = \frac{26\text{m}}{20\mu} \ln\left(\frac{0.5\text{m}}{20\mu}\right) = 4.1845 \text{ k}\Omega \quad [1]$$

$$R_O = 12.5\text{M}[1 + 0.7692\text{m}(260\text{k} || 4.1845\text{k})] = 52.05 \text{ M}\Omega \quad [1]$$

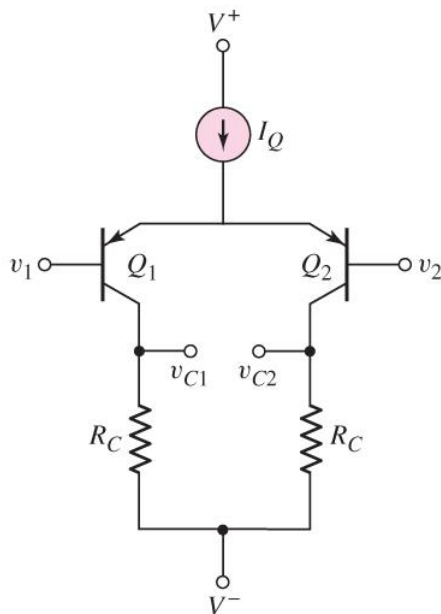
$$dI_O = \frac{dV_{C2}}{R_O} = \frac{20\mu}{52.05\text{M}} = 0.7692 \text{ mA/V} \quad [1]$$

$$dV_{C2} = 5 - 0.9 = 4.1 \text{ V} \quad [0.5]$$

$$dI_O = \frac{dV_{C2}}{R_O} = \frac{4.1}{52.05\text{M}} = 0.0787 \mu\text{A} \quad [1]$$

$$\text{Percentage change in } I_O = \frac{dI_O}{I_O} \times 100\% = \frac{0.0787\mu}{20\mu} \times 100\% = 0.394\% \quad [1]$$

Q1(b) Draw pnp diff amp [4 marks]



Correct location of devices: [1 + 1 + 1]
 current source, transistors & load R_C
 Correct connection to power supplies [1]

Q1(c) **Calculate** max value of load resistance R_C and one-sided differential gain, A_d . **[8 marks]**

$$V_E = V_{EB}(on) + V_B = 0.7 + 0 = 0.7 \text{ V} \quad [1]$$

$$\text{Also, } V_E = V_{EC} + V_C = V_{EB}(on) + V_C = 0.7 + V_C = 0.7 \text{ V} \quad [1]$$

$$\text{So, } V_C = 0 \text{ V} \quad [0.5]$$

$$V_C = I_{C1}R_C + V_- \quad [1]$$

$$I_{C1} = \frac{I_Q}{2} = \frac{0.5\text{m}}{2} = 0.25 \text{ mA} \quad [0.5]$$

$$\text{Thus, } V_C = 0 = (0.25\text{m})R_C + (-5) \rightarrow R_C = 20 \text{ k}\Omega \quad [1]$$

$$A_d = \frac{g_m R_C}{2} \quad [1]$$

$$g_m = \frac{I_{C1}}{V_T} = \frac{0.25\text{m}}{26\text{m}} = 9.615 \text{ mA/V} \quad [1]$$

$$A_d = \frac{9.615\text{m}(20\text{k})}{2} = 96.15 \text{ V/V} \quad [1]$$

Question 2 [20 marks]

Answers:

Question 2(a) [5 marks]

Option 1:

$$I_Q = \left(\frac{k'_n}{2}\right) \left(\frac{W}{L}\right)_4 (V_{GS4} - V_{TN})^2 \quad [1]$$

$$0.2m = \left(\frac{50\mu}{2}\right) (15)(V_{GS4} - 0.5)^2 \quad [1]$$

$$V_{GS4} = 1.23 \text{ V}, V_{GS3} = V_{GS4} = 1.23 \text{ V} \quad [1]$$

$$V_{GS5} = V_+ - V_- - V_{GS3} = 5 - (-5) - 1.23 = 10 - 1.23 = 8.77 \text{ V} \quad [2]$$

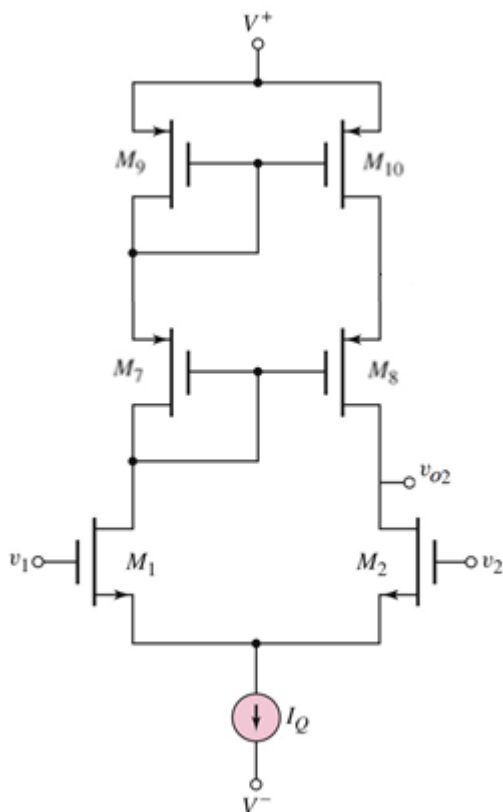
Option 2:

$$I_{D5} = I_{D3} \quad [1]$$

$$\left(\frac{50\mu}{2}\right) (3)(V_{GS5} - 0.5)^2 = \left(\frac{50\mu}{2}\right) (15)(10 - V_{GS5} - 0.5)^2 \quad [3]$$

$$V_{GS5} = 6.72 \text{ V} \quad [1]$$

Question 2(b) [5 marks]



Power supplies & connections	[2]
NMOS Diff amp	[1]
PMOS Cascode current source	[2]
Total	[5 marks]

Question 2(c) [10 marks]

Calculate A_d with passive load R_D

$$A_d = (g_{m2} R_D) / 2 \quad [1]$$

$$g_{m2} = 2\sqrt{(K_n I_Q/2)} = 2\sqrt{[(0.4\text{m})(0.2\text{m}/2)]} = \mathbf{0.4 \text{ mA/V}} \quad [1]$$

$$A_d = (\mathbf{0.4\text{m} \times 40\text{k}}) / 2 = \mathbf{8 \text{ V/V}} \quad [1]$$

Calculate A_d with Cascode active load

$$A_d = g_{m2} (r_{O2} \parallel R_{OCascode}) \quad [1]$$

$$r_{O2} = 1/(\lambda_n I_Q/2) = 1/ [(0.02)(0.2\text{m}/ 2)] = \mathbf{500 \text{ k}\Omega} \quad [1]$$

$$R_{OCascode} \approx g_{m8} r_{O8} r_{O10} \quad [1]$$

$$g_{m8} = 2\sqrt{(K_p I_Q/2)} = 2\sqrt{[(0.2\text{m})(0.2\text{m}/2)]} = \mathbf{0.2828 \text{ mA/V}} \quad [1]$$

$$r_{O8} = 1/(\lambda_p I_Q/2) = 1/ [(0.02)(0.2\text{m}/ 2)] = \mathbf{500 \text{ k}\Omega} \quad [0.5]$$

$$r_{O10} = 1/(\lambda_p I_Q/2) = 1/ [(0.02)(0.2\text{m}/ 2)] = \mathbf{500 \text{ k}\Omega} \quad [0.5]$$

$$R_{OCascode} \approx (0.2828\text{m})(500\text{k})(500\text{k}) = \mathbf{70.7 \text{ M}\Omega} \quad [0.5]$$

$$A_d = (\mathbf{0.4\text{m}})(\mathbf{500\text{k} \parallel 70.7\text{M}}) = 198.6 \text{ or } \approx 200 \text{ V/V} \quad [0.5]$$

A_d had increased = $198.6 - \mathbf{8} = 190.6 \text{ V/V}$ with Cascode active load. or

A_d had increased = $200 - \mathbf{8} = 192 \text{ V/V}$ with Cascode active load. [1]

Question 3 [20 marks]

Answers:

Question Q3(a) [10 marks]

$$I_{C1} = \frac{\beta}{1+\beta} I_{B2} = \frac{\beta}{1+\beta} \frac{I_{C2}}{\beta} = \frac{I_{C2}}{1+\beta} = \frac{1.2m}{61} = 19.67 \mu A \quad [2]$$

$$r_{\pi1} = \frac{\beta V_T}{I_{C1}} = \frac{(60)(0.026)}{19.67\mu} = 79.3 k\Omega \quad [1]$$

$$r_{\pi2} = \frac{\beta V_T}{I_{C2}} = \frac{(60)(0.026)}{1.2m} = 1.3 k\Omega \quad [1]$$

$$R_i = r_{\pi1} + (1 + \beta)r_{\pi2} \quad [1]$$

$$\rightarrow R_i = 79.3k + (61)(1.3k) = 158.6 k\Omega \quad [1]$$

$$r_{\pi3} = \frac{\beta V_T}{I_{C3}} = \frac{(60)(0.026)}{5m} = 312 \Omega \quad [1]$$

$$R_o = R_2 \parallel \left[\frac{r_{\pi3} + (R_1 \parallel r_{02})}{1+\beta} \right] \quad [1]$$

$$r_{02} = \frac{V_A}{I_{C2}} = \frac{\infty}{I_{C2}} = \infty \quad [1]$$

$$\rightarrow R_o = 5k \parallel \left[\frac{312 + (50k \parallel \infty)}{1+60} \right] = 5k \parallel 825 = 708\Omega \quad [1]$$

Question Q3(b) [2 marks]

- Class A has higher power consumption, lower efficiency than class B. [0.5]
Class B has highest efficiency but suffers from cross over distortion. [0.5]
- Class AB removes cross over distortion of Class B and, but efficiency of Class AB is lower than Class B. [0.5]
- Class A requires higher biasing current I_{CQ} compared to class AB, and has lower efficiency. [0.5]

Question Q3(c) [8 marks]

$$i_L = \frac{V_O}{R_L} = \frac{5}{100} = 50 \text{ mA} \quad [1]$$

$$i_{cn} = i_L = 50 \text{ mA} \quad [1]$$

$$V_{BE n} = V_T \ln\left(\frac{I_{Cn}}{I_S}\right) = (26\text{m}) \ln\left(\frac{50\text{m}}{10^{-13}}\right) = 0.7004 \text{ V} \quad [1]$$

$$V_{EB p} = V_{BB} - V_{BE n} = 1.35 - 0.7004 = 0.6496\text{V} \quad [0.5]$$

$$i_{cp} = I_S \exp^{V_{EB p}/V_T} = 10^{-13} \exp^{0.6496/26\text{m}} = 7.0947 \text{ mA} \quad [1]$$

$$\text{Recalculate: } i_{cn} = i_L + i_{cp} = 50\text{m} + 7.0947\text{m} = 57.0947 \text{ mA} \quad [0.5]$$

$$V_{CE n} = V_{CC} - V_O = 10 - 5 = 5 \text{ V} \quad [0.5]$$

$$V_{EC p} = V_O - (-V_{CC}) = 5 - (-10) = 15 \text{ V} \quad [0.5]$$

$$P_{Qn} = i_{cn} V_{CE n} = 57.0947\text{m} \times 5 = 285.48 \text{ mW} \quad [1]$$

$$P_{Qp} = i_{cp} V_{EC p} = 7.0947\text{m} \times 15 = 106.42 \text{ mW} \quad [1]$$

Question 4 [20 marks]

Answers:

Question Q4(a) [10 marks]

Using the equation, $I_C = I_S \exp^{V_{BE}/V_T}$ [1]

$V_{BE11} = V_{EB12} = V_T \ln\left(\frac{I_C}{I_S}\right)$ [1]

$V_{BE11} = V_{EB12} = 0.026 \ln\left(\frac{0.4 \times 10^{-3}}{5 \times 10^{-16}}\right) = 0.7126 V$ [2]

Find R_5 and R_4 ;

$R_5 = \frac{V^+ - V_{EB12} - V_{BE11} - V^-}{I_{C10}} = \frac{15 - 0.7126 - 0.7126 + 15}{0.4m} = 71.44 k\Omega$ [2]

$I_{C10}R_4 = V_T \ln \frac{I_{REF}}{I_{C10}}$ [1]

$R_4 = \frac{0.026}{0.04m} \ln \frac{0.4m}{0.04m} = 1.497 k\Omega$ [1]

$V_{BE10} = V_{BE11} - I_{C10}R_4 = 0.7126 - 0.04m(1.497k) = 0.6527 V$ [2]

Question Q4(b) [10 marks]

$A_d = g_{m2}(r_{o2} \parallel r_{o4})$ 1

$g_{m2} = \sqrt{2K_p I_Q} = \sqrt{2(100\mu)(100\mu)} = 141.42\mu A/V$ 1

$r_{o2} = \frac{1}{\lambda_p I_{D2}} = \frac{1}{0.02 \times 50\mu} = 1M\Omega$ 1

$r_{o4} = \frac{1}{\lambda_n I_{D4}} = \frac{1}{0.01 \times 50\mu} = 2M\Omega$ 1

$A_d = (141.42\mu)(1M \parallel 2M) = 94.286$ 0.5

$A_{v2} = g_{m7}(r_{o7} \parallel r_{o8})$ 1

$g_{m7} = 2\sqrt{K_{n7} I_{D7}} = 2\sqrt{(125\mu)(100\mu)} = 223.6\mu A/V$ 1

$r_{o7} = \frac{1}{\lambda_n I_{D7}} = \frac{1}{0.01 \times 100\mu} = 1M\Omega$ 1

$r_{o8} = \frac{1}{\lambda_p I_{D8}} = \frac{1}{0.02 \times 100\mu} = 0.5M\Omega$ 1

$A_{v2} = (223.6\mu)(1M \parallel 0.5M) = 74.53$ 0.5

$A_v = A_d A_{v2} = 94.286 \times 74.53 = 7027.45$ 1, 1

Question 5 [20 marks]

Answers:

Question Q5(a) [4 marks]

i)	The input impedances of both the inverting and non-inverting input terminals are infinity	[0.5].
	Since it is an open circuit, current will not flow into the input terminals.	[0.5]
ii)	Since open loop gain A_{od} is infinity,	[1]
	for a finite output voltage v_o , the differential voltage $v_d = v_2 - v_1$ is zero.	[1]
	Hence v_1 and v_2 are nearly equal, i.e. $v_1 = v_2$, which is a 'virtual short'.	[0.5]
	Both voltages v_1 & v_2 are forced to be the same without any physical connection between the terminals	[0.5].

Question Q5(b) [4 marks]

$$v_o = \left(1 + \frac{R_2}{R_1}\right) v_i = \left(1 + \frac{30k}{20k}\right) 1m = 2.5 \text{ mV} \quad [0.5, 0.5, 0.5]$$

$$v_{o1} = v_o = 2.5 \text{ mV} \quad [1]$$

$$v_{o2} = -\left(\frac{R}{R}\right) v_o = -\left(\frac{10k}{10k}\right) 2.5m = -2.5 \text{ mV} \quad [0.5, 0.5, 0.5]$$

Question Q5(c) [12 marks]

$$v_o(\text{max}) = 5 \text{ V} = A_d(\text{max}) \times V_d = 500V_d \quad [2]$$

$$V_d = V_{i1} - V_{i2} = \frac{v_o(\text{max})}{A_d(\text{max})} = \frac{5}{500} = 0.01 \text{ V} \quad [1]$$

$$V_d = i_{R1}(\text{max}) \times (\text{min}), \text{ where } R_1(\text{min}) = R_{1f} \quad [1]$$

$$0.01 = 10\mu \times R_{1f}$$

$$R_{1f} = 1 \text{ k}\Omega \quad [1]$$

$$A_d = \left(1 + \frac{2R_2}{R_{1f} + R_{1v}}\right) \left(\frac{R_4}{R_3}\right), \text{ where } \frac{R_4}{R_3} = 4 \quad [1]$$

$$A_d(\text{max}) = 500 = \left(1 + \frac{2R_2}{R_{1f}}\right) (4) = \left(1 + \frac{2R_2}{1k}\right) (4) \quad [2]$$

$$\text{So, } R_2 = 62 \text{ k}\Omega \quad [1]$$

$$A_d(\text{min}) = 10 = \left(1 + \frac{2R_2}{R_{1f} + R_{1v}}\right) (4) = \left(1 + \frac{2(62k)}{1k + R_{1v}}\right) (4) \quad [2]$$

$$\text{So, } R_{1v} = 81.67 \text{ k}\Omega \quad [1]$$