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Section Number: 01/02/03/04 A/B
Lecturer: Dr Jamaludin/Dr Fazrena Azlee
Table Number:



College of Engineering
Department of Electronics and Communication Engineering

Test 1 – Model Answers

SEMESTER 2, ACADEMIC YEAR 2018/2019

Subject Code : **EEEEB273/EEEEB2014**
Course Title : **Electronics Analysis & Design II**
Date : **1 December 2018**
Time Allowed : **2 hours**

Instructions to the candidates:

1. Write your Name and Student ID Number. Indicate your Section Number and Lecturer's Name. Write also your Table Number.
2. **Write all your answers using pen. DO NOT USE PENCIL** except for the diagram.
3. **ANSWER ALL QUESTIONS. Show all calculations clearly.** Every value or parameter **must** be written with its correct **Unit**.
4. **WRITE YOUR ANSWER ON THIS QUESTION PAPER.**

NOTE: DO NOT OPEN THE QUESTION PAPER UNTIL INSTRUCTED TO DO SO.

☺ **GOOD LUCK!** ☺

Question Number	Q1 (a-d)	Q2 (a)	Q2 (b)	Q3 (a)	Q3 (b)	Q4 (a-b)	Total
Marks							

QUESTION 1 [30 marks]

Answers for Question 1

Two-transistor current source	Three-transistor current source	Wilson current source
<p>Question 1(a) [2.5x3 marks]</p> $R_1 = (V^+ - V_{BE} - V^-) / I_{REF} \quad [1]$ $= (12 - 0.7 - (-12)) / (1.2\text{m}) \quad [1]$ $= 19.417 \text{ k}\Omega \quad [1/2]$	$R_1 = (V^+ - 2 V_{BE} - V^-) / I_{REF}$ $= (12 - 2 \times 0.7 - (-12)) / (1.2\text{m})$ $= 18.833 \text{ k}\Omega$	$R_1 = (V^+ - 2 V_{BE} - V^-) / I_{REF}$ $= (12 - 2 \times 0.7 - (-12)) / (1.2\text{m})$ $= 18.833 \text{ k}\Omega$
<p>Question 1(b) [4.5x3 marks]</p> $I_O = I_{REF} / (1 + 2/(\beta)) \quad [1]$ $= (1.2\text{m}) / (1 + 2/(40)) \quad [1/2]$ $= 1.1428 \text{ mA} \quad [1/2]$ $r_{O2} = V_A / I_O \quad [1]$ $= 120 / (1.1428\text{m}) = 105 \text{ k}\Omega$ $R_O = r_{O2} \quad [1]$ $= 105 \text{ k}\Omega \quad [1/2]$	$I_O = I_{REF} / (1 + 2/(\beta(1+\beta)))$ $= (1.2\text{m}) / (1 + 2/(40 \times 41))$ $= 1.1985 \text{ mA}$ $r_{O2} = V_A / I_O$ $= 120 / (1.1985\text{m}) = 100.12 \text{ k}\Omega$ $R_O = r_{O2}$ $= 100.12 \text{ k}\Omega$	$I_O = I_{REF} / (1 + 2/(\beta(2+\beta)))$ $= (1.2\text{m}) / (1 + 2/(40 \times 42))$ $= 1.1985 \text{ mA}$ $r_{O3} = V_A / I_O$ $= 120 / (1.1985\text{m}) = 100.12 \text{ k}\Omega$ $R_O = (\beta r_{O3}) / 2$ $= (40 \times 100.12\text{k}) / 2$ $= 2.002 \text{ M}\Omega$
<p>Question 1(c) [2x3 marks]</p> $dI_O = dV_O / R_O \quad [1]$ $= 2.3 \text{ V} / 105 \text{ k}\Omega \quad [1/2]$ $= 0.0219 \text{ mA} \quad [1/2]$	$dI_O = dV_O / R_O$ $= 2.3 \text{ V} / 100.12 \text{ k}\Omega$ $= 0.0229 \text{ mA}$	$dI_O = dV_O / R_O$ $= 2.3 \text{ V} / 2.002 \text{ M}\Omega$ $= 0.0011 \text{ mA}$

Question 1(d) [3 marks]

Most stable: Wilson, medium stable: Three-transistor, least stable: Two-transistor.

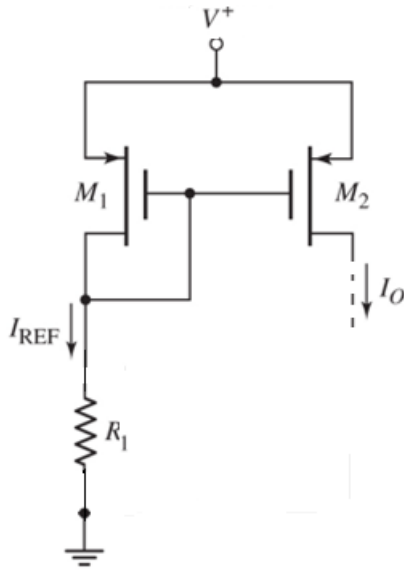
Io for Wilson is approximately equal to Iref, Ro is the highest (dIo is the smallest).

Io for 3-transistor is approximately equal to Iref but bigger than Io for 2-transistor, Ro is the similar to 2-transistor (dIo is higher compared to Wilson).

Io for 2-transistor is lower than Iref compared to 3-transistor and Wilson, Ro is the similar to 3-transistor (dIo is higher compared to Wilson).

QUESTION 2 [30 marks]

Answers for Question 2(a)



- (i) **Sketch:** [6 marks]
 - Correct connections for M1 & M2 [2 marks]
 - Correction connections for power supplies [2 marks]
 - Correct direction and placement for IREF and IO [2 marks]

- (ii) **Current relationships** [4 marks]
 - $I_O = I_{D2} = \frac{1}{2} k_n' (W/L)_2 (V_{GS2} - V_{TN})^2$ [1 mark]
 - $I_{REF} = I_{D1} = \frac{1}{2} k_n' (W/L)_1 (V_{GS1} - V_{TN})^2$ [1 mark]
 - From circuit, $V_{GS1} = V_{GS2} = V_{GS}$ [1 mark]
 - Divide I_O with I_{REF} , and common terms cancel out,
Left with current and aspect ratio terms only: [1 mark]

$$\frac{I_O}{I_{REF}} = \frac{(W/L)_2}{(W/L)_1}$$

Which is:

$$I_O = \frac{(W/L)_2}{(W/L)_1} \cdot I_{REF}$$

Answers for Question 2(b)**(i) Calculate VGS [5 marks]**

$$I_{REF} = I_{D3} = I_{D1} = 2\text{mA} \quad [1 \text{ mark}]$$

$$I_{D1} = K_{n1}(V_{GS1} - V_{TN})^2$$

$$2\text{mA} = 25\text{m}(V_{GS1} - 0.9)^2$$

$$V_{GS1} = 1.1828\text{V} \quad [1 \text{ mark}]$$

$$V_{GS2} = V_{GS1} = 1.1828\text{V} \quad [0.5 \text{ mark}]$$

$$V_{GS3} = V_{GS1} = 1.1828\text{V} \quad [0.5 \text{ mark}]$$

$$I_o = I_{D4} = I_{D2} = 40\mu\text{A}$$

$$I_{D4} = K_{n4}(V_{GS4} - V_{TN})^2 \quad [1 \text{ mark}]$$

$$40\mu\text{A} = 25\text{m}(V_{GS4} - 0.9)^2$$

$$V_{GS4} = 0.94\text{V} \quad [1 \text{ mark}]$$

(ii) Calculate (W/L) [5 marks]

$$K_{n1} = \frac{1}{2} k_n' (W/L)_1 \quad [1 \text{ mark}]$$

$$25\text{m} = \frac{1}{2} (0.5\text{m}) (W/L)_1$$

$$(W/L)_1 = 100 \quad [1 \text{ mark}]$$

$$(W/L)_3 = (W/L)_1 = 100 \quad [0.5 \text{ mark}]$$

$$(W/L)_4 = (W/L)_2 = (W/L)_1 = 100 \quad [0.5 \text{ mark}]$$

$$(W/L)_2 = [I_o / I_{REF}] \cdot (W/L)_1 \quad [1 \text{ mark}]$$

$$= [40\mu / 2\text{m}] \cdot 100 = 2 \quad [1 \text{ mark}]$$

(iii) Calculate Ro [4 marks]

$$\text{For cascode, } R_o = g_{m4} r_{o4} r_{o2} \quad [1 \text{ mark}]$$

$$g_{m4} = 2 \cdot \sqrt{K_{n4} \cdot I_{D4}}$$

$$= 2 \cdot \sqrt{(25\text{m})(40\mu)} = 2\text{mA/V} \quad [1 \text{ mark}]$$

$$r_{o4} = r_{o2} = 1 / \lambda I_{D4} = 1 / (0.02)(40\mu) = 1.25\text{M}\Omega \quad [1 \text{ mark}]$$

$$R_o = (2\text{m})(1.25\text{M})(1.25\text{M}) = 3.125\text{G}\Omega \quad [1 \text{ mark}]$$

(iv) Calculate percentage change in Io [4 marks]

$$\% \text{ change in } I_o = dI_o / I_o \times 100\% \quad [1 \text{ mark}]$$

$$dI_o = dV_{D4} / R_o \quad [1 \text{ mark}]$$

$$= 2.5 / 3.125\text{G} = 8 \times 10^{-10} = 0.8\text{ nA} \quad [1 \text{ mark}]$$

$$\% \text{ change in } I_o = 0.8\text{n} / 40\mu \times 100\%$$

$$= 2 \times 10^{-3} \% \quad [1 \text{ mark}]$$

(v) Using 2T current source [2 marks]

$$\text{The \% change in } I_o \text{ shall increase} \quad [1 \text{ mark}]$$

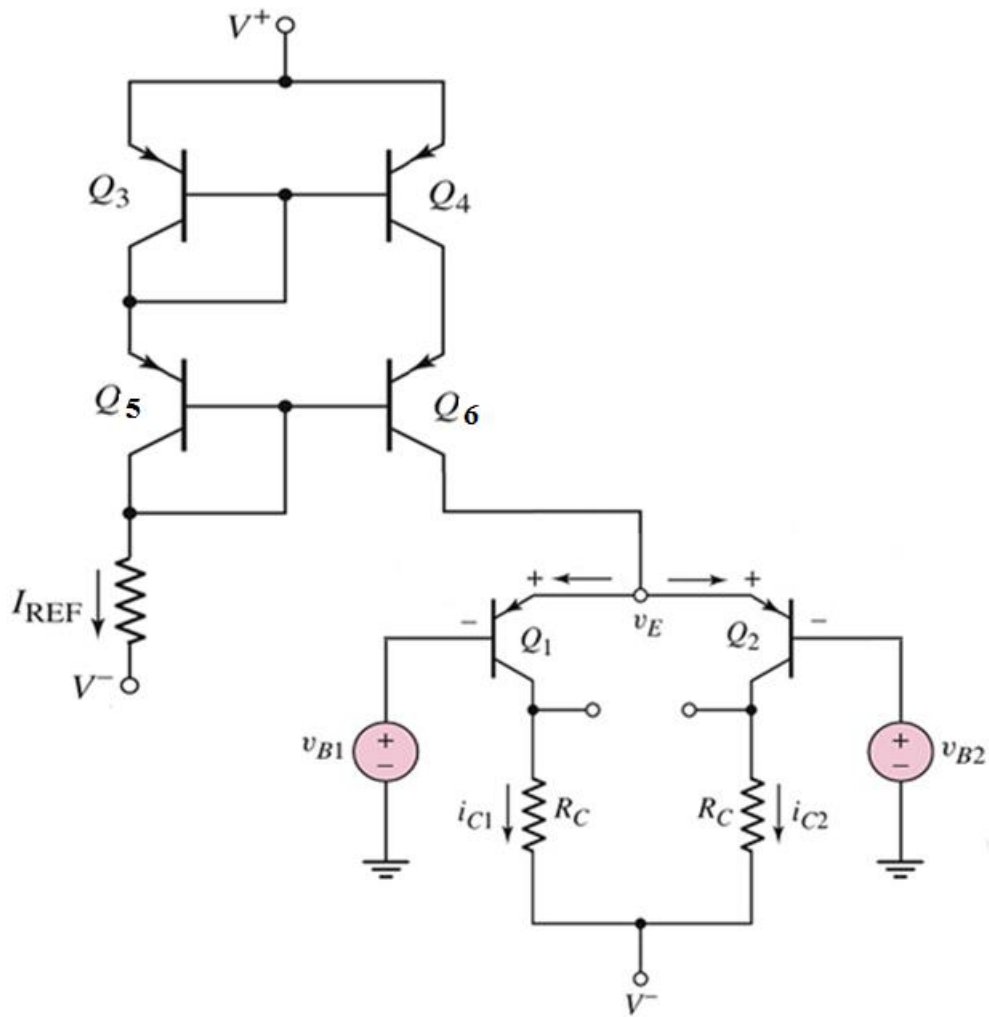
$$\text{Because 2T has lower } R_o, R_o = r_{o2} = 1.25\text{M} \quad [0.5 \text{ mark}]$$

$$dI_o = 2.5 / 1.25\text{M} = 2\text{ uA}$$

$$\% \text{ change in } I_o = 2\mu / 40\mu \times 100\% = 5 \% \quad [0.5 \text{ mark}]$$

QUESTION 3 [20 marks]

Answers for Question 3(a)



- PNP Differential amp [2]
- PNP Cascode current source [2]
- Correct connections and power supplies [1]

Total: 5 marks

Answers for Question 3(b)**Q3b(i) [5 marks]**

$$I_1 = \left(1 + \frac{2}{\beta}\right) I_Q = 4.067mA \quad [1]$$

$$I_1 = \left(1 + \frac{2}{\beta}\right) (4mA) = 4.067mA \quad [1.5]$$

$$R_1 = \frac{V^+ - V_{BE} - V^-}{I_1} = 4.75k\Omega \quad [1]$$

$$R_1 = \frac{10 - 0.7 - (-10)}{4.067mA} = 4.75k\Omega \quad [1.5]$$

Q3b(ii) [5 marks]

$$I_{E2} = \frac{I_Q}{2} = \frac{4mA}{2} = 2mA \quad [1]$$

$$I_{C2} = \frac{\beta}{1+\beta} I_{E2} = 1.983mA \quad [1.5]$$

$$V_{O2} = V^+ - I_{C2}R_C \quad [1.5]$$

$$V_{O2} = 10 - (1.983mA)(5k) = 0.085V \quad [1]$$

Q3b(iii) [5 marks]

$$V_{CE4} = V_{C4} - V_{E4} = (V_1 - V_{BE1}) - V^- \quad [3]$$

$$V_{CE4} = 0 - 0.7 - (-10) = 9.3V \quad [2]$$

QUESTION 4 [20 marks]**Answers for Question 4****(a) Calculate A_d , A_{cm} and CMRR in dB [13 marks]**

$$I_{REF} = (V_+ - V_{BE} - V_-) / R_1 = (10 - 0.7) / 37k = 0.2514mA \quad [2 \text{ marks}]$$

$$I_Q = I_{C4} = I_{REF} / [1 + 2/B] = 0.2514mA / [1 + 2/250] = 0.2494mA \quad [2 \text{ marks}]$$

$$I_1 = I_2 = I_Q / 2 = 0.2494mA / 2 = 0.1247mA \quad [1 \text{ mark}]$$

$$G_m = I_1 / V_T = 0.1247mA / 26m = 4.796mA/V \quad [1 \text{ mark}]$$

$$R_\pi = B V_T / I_1 = 250.26m / 0.1247mA = 52.124k\Omega \quad [1 \text{ mark}]$$

$$A_d = B R_c / [2(r_\pi + R_B)] = 250.30k / [2(52.124k + 500)] = 71.2588V/V \quad [1.5 \text{ mark}]$$

$$R_o \text{ of } 2T = r_{o4} = V_{A3} / I_Q = 100 / 0.2494mA = 400.96k\Omega \quad [1 \text{ mark}]$$

$$A_{cm} = -g_m R_c / [1 + 2(1+B)R_o / (r_\pi + R_B)] = -4.796mA/V (30k) / [1 + 2(251)(400.96k) / (52.124k + 500)] = -0.0376 V/V \quad [1.5 \text{ mark}]$$

$$\text{CMRR in dB} = 20 \log_{10}[A_d / A_{cm}] = 20 \log_{10}[71.2588 / 0.0376] = 65.55dB \quad [1 \text{ mark}]$$

(b) Calculate output voltage [7 marks]

$$V_d = v_1 - v_2 = 210 \times 10^{-6} \sin \omega t \text{ V} - 190 \times 10^{-6} \sin \omega t \text{ V} = 20 \times 10^{-6} \sin \omega t \text{ V} \quad [2 \text{ marks}]$$

$$V_{cm} = [v_1 + v_2] / 2 = [210 \times 10^{-6} \sin \omega t \text{ V} + 190 \times 10^{-6} \sin \omega t \text{ V}] / 2 = 200 \times 10^{-6} \sin \omega t \text{ V} \quad [2 \text{ marks}]$$

Output voltage,

$$v_o = A_d V_d + A_{cm} V_{cm} \quad [2 \text{ marks}]$$

$$= (71.2588)(20 \times 10^{-6} \sin \omega t \text{ V}) + (-0.0376)(200 \times 10^{-6} \sin \omega t \text{ V}) = 1.4177 \times 10^{-3} \sin \omega t \text{ V} \quad [1 \text{ mark}]$$